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No evidence for younger stellar generations within the intermediate-age massive clusters NGC 1783, NGC 1806 and NGC 411

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ABSTRACT

Recently, Li et al. claimed to have found evidence for multiple generations of stars in the intermediate-age clusters NGC 1783, NGC 1806 and NGC 411 in the Large and Small Magellanic Clouds. Here we show that these young stellar populations are present in the field regions around these clusters and are not likely associated with the clusters themselves. Using the same data sets, we find that the background subtraction method adopted by the authors does not adequately remove contaminating stars in the small number Poisson limit. Hence, we conclude that their results do not provide evidence of young generations of stars within these clusters.

Key words: globular clusters: general – galaxies: star clusters: general – galaxies: star clusters: individual: NGC 1783, NGC 1806, NGC 411.

1 INTRODUCTION

The peculiar abundance patterns found in globular clusters, and the complex colour–magnitude diagrams (CMDs) of young and intermediate-age clusters in the Magellanic Clouds have turned the study of multiple stellar populations (MPs) in clusters into a very active research field. Often, these MPs have been hypothesized to be associated with different stellar generations – i.e. distinct epochs of star formation (e.g. Mackey et al. 2008 in the context of intermediate-age clusters in the Magellanic Clouds). However, definitive evidence for multiple stellar generations within stellar cluster remains elusive to date¹ (cf. Cabrera-Ziri et al. 2014, 2016; Li, de Grijs & Deng 2014; Niederhofer et al. 2015).

Recently, Li et al. (2016; hereafter L16), studied the CMDs of three intermediate-age (~ 1.5 Gyr) clusters in the LMC/SMC

(NGC 1783, NGC 1806² and NGC 411), and claimed to have found young (few hundred Myr) populations of stars in each cluster. The authors interpreted these results as a ‘smoking gun’ of a recent star formation burst within these clusters.

In this paper, we use L16 photometric catalogues, and find that the young populations on the CMDs of these three clusters are also present in the CMDs of field regions around the clusters, challenging the associations of the young populations with these clusters.

2 DENSITIES AND LUMINOSITY FUNCTIONS OF THE YOUNG STARS

We compared the density of young stars in the cluster (i.e. inner two core radii, as defined by L16) and in the reference field region, which was chosen to be the same as in L16. This comparison was done before applying any decontamination and the definition of the young sequences in the CMD was selected to be $B(\text{mag}) < \{21.25,$

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¹ With the notable exception of nuclear stars clusters e.g. Walcher et al. (2006).

² In Li et al. catalogs NGC 1806 was attributed the wrong ID, i.e. NGC 1696. In the catalogs the coordinates match that of NGC 1806 and NGC 411.

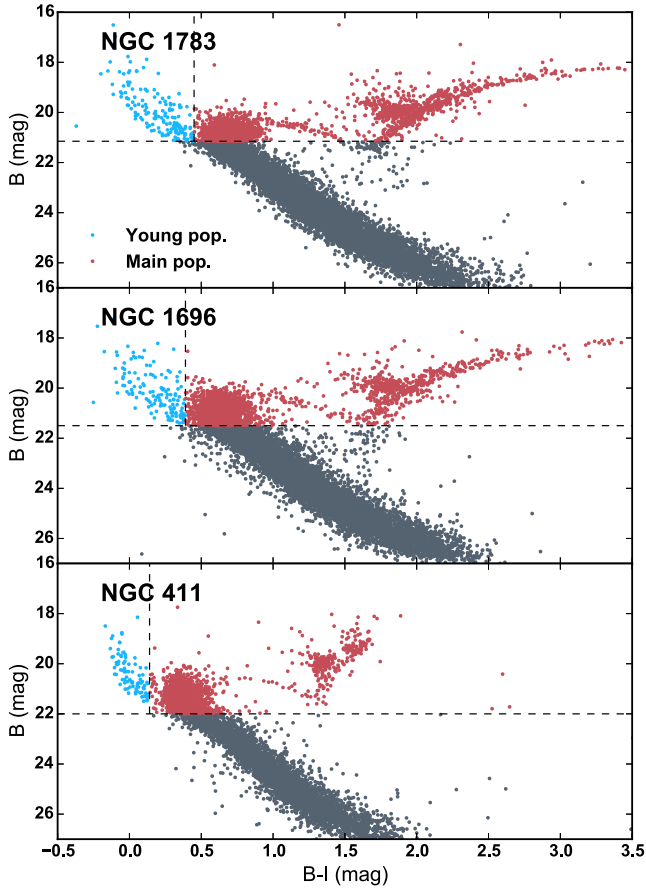


Figure 1. Selection of young (blue dots) and main (~ 1.5 Gyr old – red dots) populations from the CMDs (before decontamination) for the LFs (cf. Fig. 2) and radial profiles (cf. Fig. 8).

$21.50, 22.00\}$ and $B - I(\text{mag}) < \{0.45, 0.39, 0.14\}$ for clusters NGC 1783, NGC 1806 and NGC 411 respectively (cf. Fig. 1). In Table 1 we report the number and (average) surface density of the young stars in the cluster and reference field region for each case. In brackets we show the standard deviation of the densities calculated \sqrt{N}/A_C and $\sqrt{N_F}/A_F$ where A_C and A_F are the solid angle (area) of the cluster and reference field region.

The last column of the table shows the difference between surface densities. For NGC 1783, we find that the reference field contains significantly ($\sim 4\sigma$) more of these young stars per unit area than the cluster. While for NGC 1806 and NGC 411 both the densities of young stars in the cluster is 0 within $\sim 2.3\sigma$ and $\sim 1.9\sigma$, respectively. From this, we find no significant overdensities of young stars in the cluster regions with respect to the reference field.

Additionally, we calculated the luminosity functions (LFs) of these young populations in the field region and compared them with the LFs of the young populations in the cluster region (also before applying any decontamination). The cumulative LFs of the young

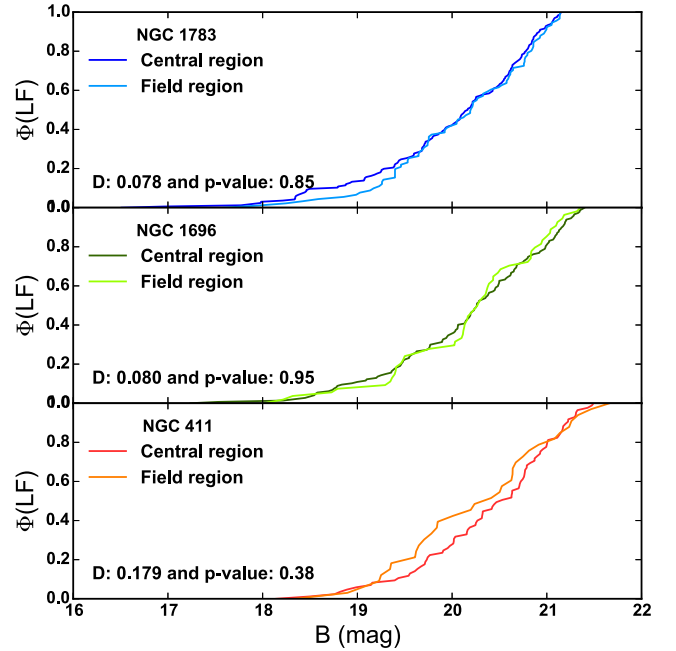


Figure 2. Cumulative LFs of the young populations in the clusters and field regions. In each panel we report the KS statistic, D , and p -value from our analysis of the LFs of the young populations from the field and cluster regions. We find no significant differences between them.

populations from clusters and field regions are shown in Fig. 2. They are very similar in all cases. For every cluster we applied a KS test to compare the LFs of both regions, the results are shown in Fig. 2 as well. From the KS test we can say that the LFs of the young populations in the field regions around the clusters, and the LFs of the stars within the clusters, do not show any significant difference.

This casts doubts on the association of these young populations with the clusters themselves as (1) there are no obvious overdensities of young stars in the cluster with respect to the reference fields, and (2) the LFs of the young populations in the cluster region do not show a significant difference to the ones in the reference field.

3 REDUCING BACKGROUND CONTAMINATION IN L16

To remove the background contamination in the CMDs of the clusters, L16 used the following technique.

- (i) The CMD of the cluster and field region are gridded in several bins/cells.
- (ii) The number of stars within each grid cell in the field region CMD are counted.
- (iii) In the cluster region CMD, the same number of stars as in the corresponding grid cell of the field region CMD are randomly removed, accounting for the difference in solid angle (area) between the cluster and field regions.

Table 1. Number (N and N_F) and surface density (Σ_N and Σ_{N_F}) of young stars in the cluster region (before decontamination) and the reference field.

NGC	N (stars)	N_F (stars)	Σ_N ($\times 10^{-3}$ stars arcsec $^{-2}$)	Σ_{N_F} ($\times 10^{-3}$ stars arcsec $^{-2}$)	$\Sigma_{N_F} - \Sigma_N$ ($\times 10^{-3}$ stars arcsec $^{-2}$)
1783	167	311	5.32(± 0.41)	7.77(± 0.44)	-2.49(± 0.60)
1696	148	55	13.09(± 1.08)	9.17(± 1.24)	3.92(± 1.64)
411	86	34	10.95(± 1.18)	7.59(± 1.30)	3.36(± 1.76)

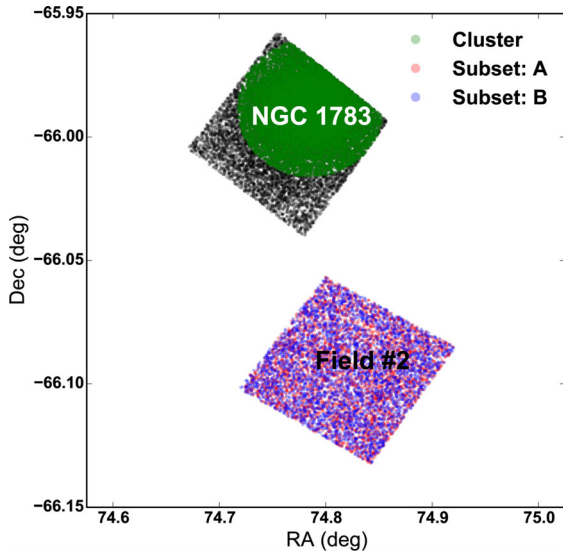


Figure 3. Spatial distribution of the cluster and field stars used in our experiments. Red and blue colours show the position of the stars from subset A and B, respectively.

(iv) The resulting subset of stars in the cluster CMD is considered the decontaminated CMD of the cluster.

This technique will perform well, i.e. reducing significantly the contribution of field stars, only in well populated grid cells, where Poisson uncertainties are much smaller than the number of available stars. However, if the grid cells are populated with just a few stars, the performance of this technique can be very poor. Another caveat of this method is that grid cells that contain more field stars than cluster stars end up with negative values, which are not taken into account during the analysis. This is the case of the regions of the CMDs that host the young population of the LMC/SMC field (i.e. these regions contain both positive and negative counts after using this technique).

4 PERFORMANCE OF L16 BACKGROUND DECONTAMINATION

4.1 Subtracting the field from the field

To illustrate the flaw of the technique used by L16, we carry out a simple experiment. For this we have randomly assigned the stars of the L16 field region to two subsets, irrespective of their spatial location. The experiment consists of taking these two subsets of stars, and applying the L16 method to reduce the background using one subset as a primary field and the other as reference/background population. With this experiment one would expect to find very few stars at the end, as we are subtracting populations that are statistically identical. If on the contrary, we find that this test yields significant residuals, one can conclude that the technique used is not adequate.

For these experiments we have used the same grid/binning as L16, i.e. grid cells of magnitude \times colour = $0.5 \times 0.25 \text{ mag}^2$ ranging from $(B - I) = -2.5 \text{ mag}$ to 3.5 and $B = 16$ to 27 mag .

In Fig. 3, we show the spatial distribution of the subsets of stars taken for our experiment. The subsets A and B, have the same number of stars and were chosen randomly. Both are distributed uniformly across the field region next to the cluster NGC 1783. The CMDs of both subsets are shown respectively in panels ‘A’ and ‘B’ of Fig. 4. The CMDs are virtually identical. As noted in Section 2, the young populations found in L16 are already present in the field region. We show the Marigo et al. (2008) isochrones attributed by L16 to each population for reference. The colour scale represents the log of the number of stars in each grid element.

We then proceed with our experiment, assuming that the subset A contains stars that belong to the primary field, and subset B stars form the reference/background region. After applying the technique used by L16, we were left with the CMD shown in panel ‘A-B’ of Fig. 4.

In this ‘residual’ CMD we note that this technique was efficient in removing most of the stars along the field’s MS, i.e. stars with

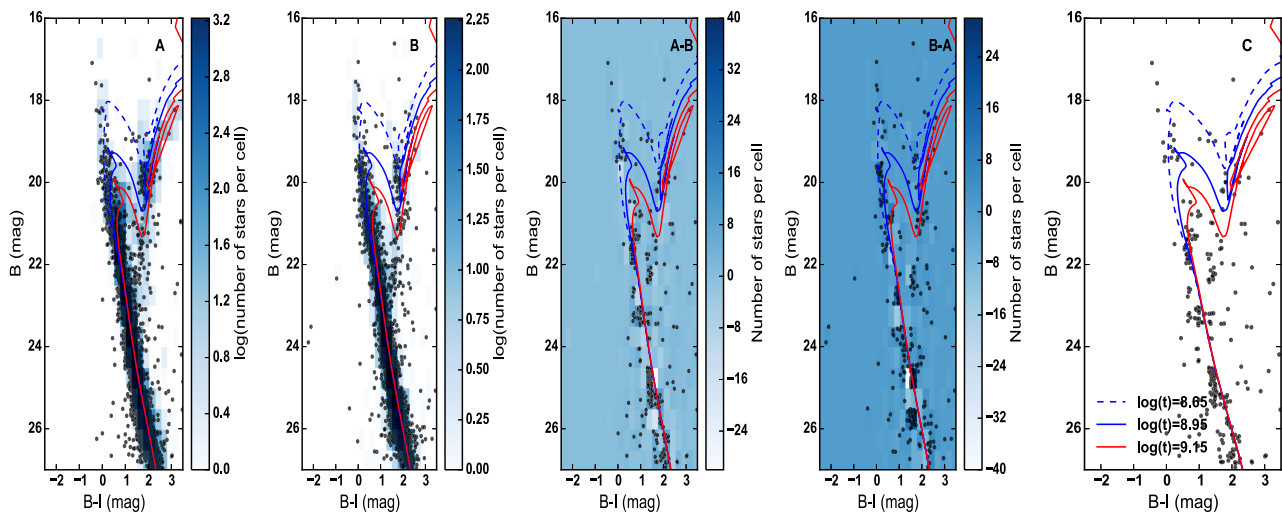


Figure 4. CMDs of subset A and B are shown in panels ‘A’ and ‘B’, respectively. The colour scales in these two panels show the log of the number of stars in each grid element. Panel ‘A-B’ shows the residual CMDs obtained when we applied L16’s decontamination method assuming that subset A represents the CMD of the stars in the primary field and subset B the reference/background stars. Panel ‘B-A’ is similar to panel ‘A-B’ but here subset B was taken as the stars in the primary field and subset A the reference stars instead. The colour scale of panels ‘A-B’ and ‘B-A’ show the number of stars in each grid cell in linear scale. Panel ‘C’ is the same as panel ‘A-B’, but without the colour scale. The isochrones in all panels are the same attributed by L16 to the young sequences in their CMD of NGC 1783.

$B > 22$ mag. In these regions we are left with $\pm \sim 15$ stars/cell – the negative values correspond to grid cells where there are not enough stars to subtract, i.e. fewer stars in the grid cells of the primary than in the reference/background region, more on this in Section 5. When we compare these values to the original number of stars in these grid cells ~ 200 (i.e. before applying the decontamination technique), we are left with about ~ 8 per cent of the original number of stars in this region of the CMD.

On the other hand, there are significantly fewer stars close to the turn-off of the young populations ($B < 20$ mag) with ~ 5 stars/cell in comparison to ~ 200 stars/cell in the fainter part of the CMD. The problem with the decontamination method used by L16 is particularly evident here. After ‘decontaminating’ this part of the CMD, the number of stars per grid cell does not change much – there are still ± 5 stars/cell. In other words, the residuals after decontamination are comparable to the original population due to low number statistics.

The same result is obtained if we take as primary-field stars the background population B and use background population A as reference-field stars, as shown in panel ‘B-A’ of the same figure. In this technique, only grid cells with positive counts are analysed, i.e. grid cells resulting in negative counts are ignored, resulting in a bias in the analysis.

We have carried out similar tests, defining different subsets of stars A and B. Also, we have divided ‘Field #2’ (cf. Fig. 3) in different spatial subsets, and carried out the same experiments in each of them. All our tests show the same results: the residuals of the young populations are present after the statistical decontamination.

We find the same results for NGC 1806 and NGC 411, the other clusters studied by L16. The presence of these residuals after our experiments also calls into question the association of the young populations with these clusters, as they show the ‘noise’ leftover after decontaminating a CMD with this technique.

4.2 Decontaminating the cluster CMD

We have applied L16’s method to decontaminate the CMD of the clusters using the same reference field as L16 and the same CMD grids. The results obtained for NGC 1783 are shown in Fig. 5.

The red cells in this figure represent ‘negative cells’, i.e. the cells where the number of stars of the reference field CMD was greater than the number of stars in the cluster region CMD. This feature, ‘the negative stars’, is intrinsic to L16’s decontamination technique and is a direct consequence of the Poisson regime, where the error in the number of counts is of the order of the number of counts itself. In Fig. 4, this is clearly observed when we compare panels ‘A-B’ and ‘B-A’, as the ‘negative stars’ that are missing in one CMD are observed in the other. As a consequence of this effect we have the gaps in the CMDs observed in the panels ‘A-B’, ‘B-A’ and ‘C’ of Fig. 4. In Fig. 5, this is responsible for the gaps in the faint end of the MS of NGC 1783. Similar effects were readily observed in the first figure of L16, where the younger populations following the isochrones (square symbols) do not show stars below a certain threshold in B magnitude. This gap is not expected if these younger populations follow conventional initial mass functions, so it is likely that the ‘gaps’ simply represent ‘negative star’ counts.

5 SIGNIFICANCE OF THE L16 DETECTIONS

We used the method outlined in Knoetig (2014) to calculate the probability of the stars in the on-cluster CMD to belong to the background/field and also to quantify the significance of the detections. The solution presented by Knoetig assumes that the on-

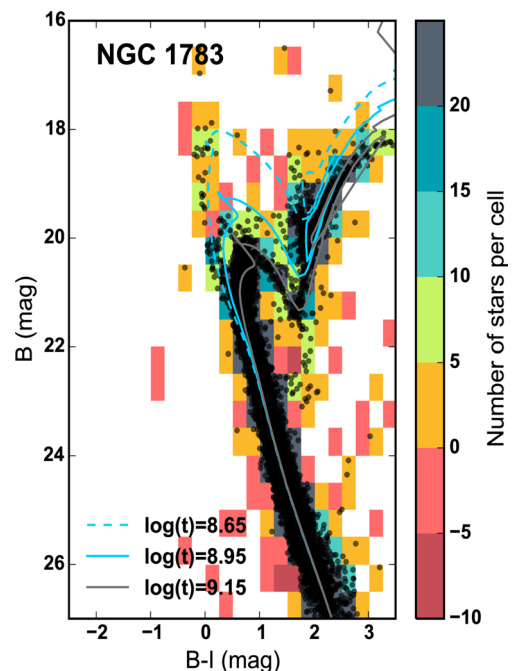


Figure 5. CMD of NGC 1783 produced by L16’s decontamination technique. In colour, we represent the number of star/cell. The negative values represent the grid cells where there were more stars in the reference field than in the cluster region.

and off-cluster cell counts follow a Poissonian distribution, and this method has the advantage to be applicable to cells with small and large number of counts, which is ideal in our case, as the number of counts in a cell changes significantly across the CMDs as shown in Section 4. We refer the reader interested in the details of this method to Knoetig (2014), as the discussion of such a rigorous analysis escapes the scope of this paper.

This method depends only on three parameters: the number of stars in a cell of the on-cluster CMD, the number of stars in a cell of the off-cluster (background/reference) CMD, and the ratio of exposure times between the on- and off-cluster pointings, α . We have adopted $\alpha = 1$, as is adequate to the regions of the CMD we are interested in, i.e. the ones hosting the young populations, however this assumption need not necessarily be correct for the faint end of the CMD where incompleteness might play a role due to the different exposure times (minimum and maximum exposure times between the on- and off-cluster pointings are 680 s and 720 s, respectively).

We use equation 23 in Knoetig (2014), to calculate the probability of the cell counts in the on-cluster CMD to be only due to background/field stars. In Fig. 6, we show the raw CMD of NGC 1783 (i.e. before decontamination), and in colour we represent the (log of the) probability of the stars in the on-cluster region to belong to the background/LMC-field population. Note that all cells that do not belong to the main (~ 1.5 Gyr) population, have large (~ 10 –85 per cent) probabilities to belong to the LMC field. On the other hand, the probability that stars along the main cluster sequence belong to the LMC field is vanishingly small, less than 10^{-4} per cent and as small as 10^{-31} per cent along the main sequence.³

We have also calculated the significance of the detections, S_b , defined as ‘if the probability were normally distributed, it would

³ Note that the colour scale in Fig. 6 is truncated to highlight the contrast between the young and main population.

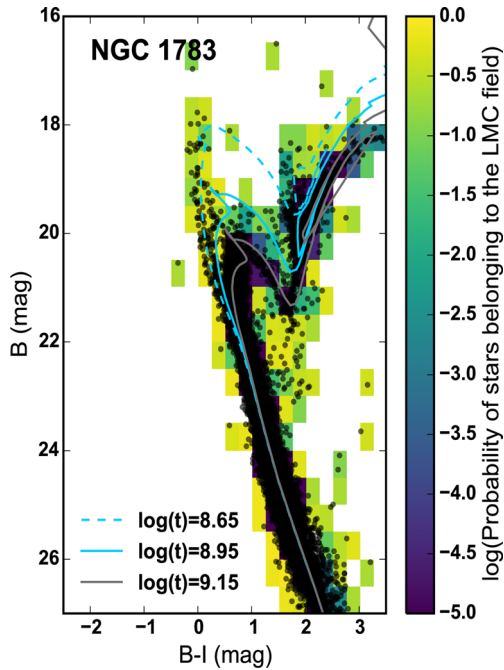


Figure 6. On-cluster CMD of NGC 1783, before decontamination. The colour scale represents the log of the probability of the stars in a given cell to belong to the LMC field. The main population has very low probabilities while the young population is very likely to be members of the LMC-field.

correspond to a S_b standard deviation measurement' (equation 27 in Knoetig 2014). In other words, it quantifies how much, in standard deviation (σ) units, the number of stars in a CMD cells differs from the LMC field population. Fig. 7 shows the significance S_b of the detection of stars in a given cell with respect to the LMC field for NGC 1783. The young populations are detected with low (0–2) significance, while the main population is detected at high (>5) significance.

The probability of the young populations to belong to the background/field population and significance of the detections of the young population with respect to the reference field, calculated in this section, also suggest that the young populations from the cluster CMDs belong to the surrounding field.

6 SPATIAL DISTRIBUTION OF THE POPULATIONS

Finally, here we analyse the spatial distributions of young populations in these clusters. In Fig. 8, we have the radial profiles of the main population, i.e. intermediate-age population, and the young populations found in the clusters' region before and after CMD decontamination by L16's method. The main populations were taken from $B(\text{mag}) < \{21.25, 21.50, 22.00\}$ and $B - I(\text{mag}) \geq \{0.45, 0.39, 0.14\}$ in the CMDs for clusters NGC 1783, NGC 1806 and NGC 411, respectively (cf. Fig. 1), and the young populations were selected from the same regions as for the LFs in Section 2.

From this figure we see that these young populations seem to be less centrally concentrated with respect to the main population of the clusters, in agreement with L16's findings. For comparison, we have distributed randomly, in a statistically uniform way across each cluster (i.e. inner two core radii), 10 000 artificial stars. We then perform a KS test comparing the radial profiles of the artificial stars (uniformly distributed in space), and the radial profiles of

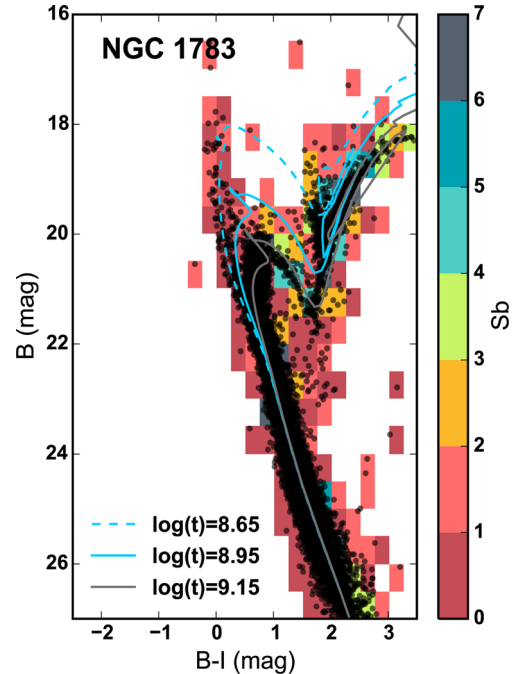


Figure 7. On-cluster CMD of NGC 1783, before decontamination. The colour scale represents the significance of the detection in a given cell with respect to the LMC field. The main population is detected at high (>5) significance. On the other hand, the significance of the detection of the young population is minimal, i.e. consistent with the LMC field.

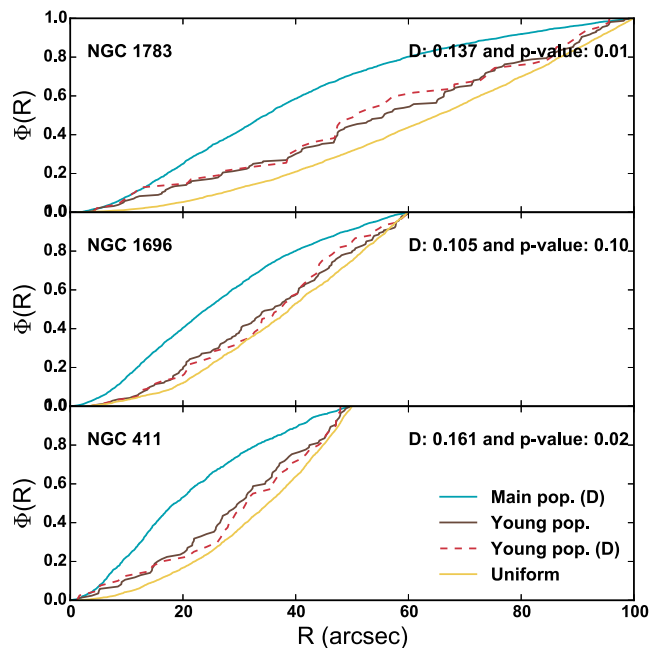


Figure 8. Radial profiles of the populations within the clusters. Blue lines: main intermediate-age population after CMD decontamination. Brown and pink lines: young populations, before and after applying L16's decontamination method. Yellow line: synthetic stars distributed uniformly across the clusters. The radial profile of the young populations in these clusters is significantly less centrally concentrated than the main population.

the young populations before any decontamination. The results of these tests are also shown in Fig. 8. We conclude that the radial profile of the young population in NGC 1806 is consistent with the radial profile of a uniform distribution of stars, as expected for field (i.e. background/foreground) stars. On the other hand, while the spatial distribution of young stars within NGC 1783 and 411 is not consistent with an uniform spatial distribution, these young stars are significantly less centrally concentrated than the main population of the cluster. We might not expect the young population to be perfectly described by a uniform population, even if they are (as we argue here) likely members of background, if there is a population gradient across the field.

The fact that the young populations found in L16's results, are significantly less centrally concentrated than the main population stars, represents another reason to question the association of these young populations to these clusters. Moreover, the young population in NGC 1806 even shares the radial profile expected for uniformly distributed field stars. This is also in agreement with the results presented in Sections 2, 4 and 5.

We note that the exact shape of the young sequences depends on the reference field adopted and the choice of bin size. On the other hand, these changes have little to no impact to the main (i.e. intermediate-age) population of these clusters.

7 SUMMARY AND CONCLUSIONS

We have re-analysed the CMDs of three intermediate-age LMC/SMC star clusters that have been recently claimed to host new generations of stars by L16. Using the same data as L16, we have shown that these young stellar populations belong to the field population of the LMC/SMC. Our experiments have shown that an insufficient background subtraction resulted in these young populations remaining in the clusters' CMDs. We conclude that L16 results are not evidence that these clusters host new generations of stars. This is consistent with previous studies that have looked for, but have not found evidence of multiple epochs of star formation within young and intermediate-age clusters, like: Bastian et al. (2013), Li et al. (2014), Cabrera-Ziri et al. (2014), Cabrera-Ziri et al. (2016), Niederhofer et al. (2015).

More sophisticated methods exist to address the issue of field contamination. In the same class as the method adopted by L16 there are applications that properly address the issues of bin edges and placements by taking into account magnitude and colour uncertainties (e.g. Kerber et al. 2002; Balbinot et al. 2010). However, more robust methods can be found that adopt an 'unbinned' approach in a matched-filter framework. Implementations of the latter methods are widely spread across the Local Group dwarf galaxy and stellar stream communities (e.g. Martin, de Jong & Rix 2008; Bechtol et al. 2015).

Having said this, given that in all cases we would be dealing with populations in the Poisson regime, one needs to be cautious when interpreting any result obtained for such populations.

In L16, the authors proposed that these clusters were able to accrete and retain gas from their surroundings (adopting the models of Conroy & Spergel 2011), which subsequently spawned a new generation of stars. Gas accretion and the gas content of star clusters have been studied in several different contexts. So far the evidence points to clusters becoming gas free at very early ages, in most cases just after a few Myr, e.g. Hollyhead et al. (2015). Other studies have shown that clusters remain gas free, even if they are, in principle (based on escape velocity arguments), massive enough to accrete and retain gas from the surrounding, up to very old ages (e.g. Bastian & Strader 2014; Bastian, Hollyhead & Cabrera-Ziri 2014; Cabrera-

Ziri et al. 2015, 2016; McDonald & Zijlstra 2015). All this suggests that stellar clusters are extremely inefficient holding on to gas within them. Perhaps this is the reason why, to date, we have not found compelling evidence for multiple stellar generations within clusters.

We note that L16 found that the 'young' stars in each of the clusters were significantly less centrally concentrated than the main stellar population, in contrast with expectations of models that invoke multiple epochs of star formation in clusters (e.g. Conroy & Spergel 2011). However, if these stars are field contaminants, as argued in the current work, the similar less centrally concentrated distribution is consistent with a field population that was not fully subtracted.

Finally, L16 adopt He enriched isochrones to explain the younger generation of stars in two of the three clusters, as standard isochrones did not fit the data (for the adopted distance and extinction of the cluster). Why material accreted from the ISM would be He enriched (and why we do not see stars forming He enriched in the field or clusters/associations today) is left unanswered.

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