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inbreedR: An R package for the analysis of inbreeding based on genetic markers

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Summary

1. Heterozygosity fitness correlations (HFCs) have been used extensively to explore the impact of inbreeding on individual fitness. Initially, most studies used small panels of microsatellites, but more recently with the advent of next generation sequencing, large SNP datasets are becoming increasingly available and these provide greater power and precision to quantify the impact of inbreeding on fitness.

2. Despite the popularity of HFC studies, effect sizes tend to be rather small. One reason for this may be a low variation in inbreeding level across individuals. Using genetic markers, it is possible to measure variance in inbreeding through the strength of correlation in heterozygosity across marker loci, termed identity disequilibrium (ID).

3. ID can be quantified using the measure g_2 which is also a central parameter in HFC theory that can be used within a wider framework to estimate the direct impact of inbreeding on both marker heterozygosity and fitness. However, no software exists to calculate g_2 for large SNP datasets nor to implement this framework.

4. **inbreedR** is an R package that provides functions to calculate g_2 based on microsatellite and SNP markers with associated p -values and confidence intervals. Within the framework of HFC theory, **inbreedR** also estimates the impact of inbreeding on marker heterozygosity and fitness. Moreover, we implemented easy-to-use simulations to explore the precision and magnitude of estimates based on different numbers of genetic markers. We hope this package will facilitate good practice in the analysis of HFCs and help to deepen our understanding of inbreeding effects in natural populations.

Key-words: inbreeding, genetic marker, HFC, heterozygosity, identity disequilibrium

32 **Introduction**

33 Offspring of close relatives often show reduced fitness, a phenomenon referred to as inbreeding depression
34 (Charlesworth & Charlesworth 1987; Charlesworth & Willis 2009). This decline in fitness among inbred
35 individuals is a result of the increased proportion of loci in the genome that are identical by descent (IBD).
36 A homozygous locus is IBD or autozygous when it carries two alleles that both originate from a single copy
37 in a common ancestor. An increased proportion of loci in the genome that are identical by descent (IBD_G)
38 may lead to the unmasking of deleterious recessive alleles and a reduction in heterozygote advantage
39 by decreasing genome-wide heterozygosity (Charlesworth & Charlesworth 1987; Charlesworth & Willis
40 2009). In populations with unknown pedigrees, many studies have used genetic marker heterozygosity
41 as a measure of IBD_G . The result is a large and expanding literature describing heterozygosity-fitness
42 correlations (HFCs) across a range of species and traits (Coltman & Slate 2003; Chapman *et al.* 2009;
43 Szulkin *et al.* 2010).

44 Despite the large and growing number of HFC studies, effect sizes are usually small (Chapman *et al.* 2009)
45 and there has been debate over their mechanistic basis (Balloux *et al.* 2004; Hansson & Westerberg 2007;
46 Slate *et al.* 2004; Szulkin *et al.* 2010). This reflects the fact that under many circumstances multilocus
47 heterozygosity based on the 10-20 microsatellite markers employed by most studies provides little power
48 to estimate IBD_G (Hansson & Westerberg 2002; Balloux *et al.* 2004; Szulkin *et al.* 2010; Hoffman *et al.*
49 2014). This is why the pedigree derived inbreeding coefficient (F_P) has long been the gold standard
50 for estimating IBD_G (Pemberton 2004; 2008). F_P is defined as the probability of a given locus in an
51 individual's genome being autozygous based on its pedigree. However, an individual's F_P will differ from
52 its IBD_G as F_P can be imprecise due to linkage among loci and downwardly biased due to incomplete
53 pedigree information (Hill & Weir 2011a; Keller *et al.* 2011; Kardos *et al.* 2015). Consequently, IBD_G
54 can vary substantially among individuals with the same F_P (Franklin 1977; Hill & Weir 2011b; Forstmeier
55 *et al.* 2012). In other words, even F_P derived from a perfect pedigree cannot fully capture the variance in
56 genomic autozygosity ($\sigma^2(IBD_G)$) among individuals, as it does not incorporate variation due to linkage.

57 Recent advances in next generation sequencing technology (e.g. Baird *et al.* 2008; Peterson *et al.* 2012)
58 now allow many tens or even hundreds of thousands of single nucleotide polymorphisms (SNPs) to be
59 genotyped in virtually any organism. Applied to HFCs, these dense marker panels provide much greater
60 power than a small panel of microsatellites to quantify the impact of inbreeding on fitness (Hoffman
61 *et al.* 2014). Recent simulation and empirical studies also show that inbreeding coefficients based on
62 genome-wide SNP data provide more precise measures of IBD_G and inbreeding depression than F_P
63 (Keller *et al.* 2011; Pryce *et al.* 2014; Kardos *et al.* 2015; Huisman *et al.* 2016).

64 **HFC theory**

65 For marker loci to indicate inbreeding depression, their heterozygosity must be correlated with the
66 heterozygosity of functional loci in the genome (Szulkin *et al.* 2010). Such correlations between marker
67 loci and functional loci have been proposed to occur through two possible mechanisms: The 'general
68 effect hypothesis' on the one hand assumes that multilocus heterozygosity (MLH) reflects genome-wide
69 heterozygosity. This association emerges because variation in inbreeding causes heterozygosity to be
70 correlated across loci, a phenomenon termed identity disequilibrium (ID, Weir & Cockerham 1973).
71 Alternatively, the 'local effect hypothesis' states that one or a few of the markers are in linkage disequilibrium
72 (LD) with a trait locus under balancing selection, which creates a pattern whereby heterozygosity at the
73 gene and marker are correlated. However, ID and LD do not necessarily have to be considered as
74 competing hypotheses to explain HFCs as ID is a consequence and LD is a cause of variation in IBD_G
75 (Bierne *et al.* 2000; Szulkin *et al.* 2010). Both mechanisms can therefore be united under an inbreeding
76 or general effect model (Bierne *et al.* 2000). Variance in individual inbreeding levels can be caused by a
77 variety of scenarios other than systematic consanguineous matings (Szulkin *et al.* 2010). For example,
78 in small or bottlenecked populations, variance in $\sigma^2(IBD_G)$ and therefore ID occurs as a consequence of
79 variation in the relatedness of mating partners. Similarly, immigration and admixture can result in the
80 offspring of parents from different populations being relatively outbred, leading to an increased $\sigma^2(IBD_G)$
81 within a population (Tsitroni *et al.* 2001; Szulkin *et al.* 2010). In addition, in small randomly mating
82 populations, both genetic drift and immigration generate LD (Hill & Robertson 1968; Sved 1968; Bierne
83 *et al.* 2000), which in turn leads to ID (Szulkin *et al.* 2010). All of these scenarios ultimately increase
84 $\sigma^2(IBD_G)$ and lead to ID, which is the fundamental cause of HFCs according to the general effect model.

85 The general effect model assumes that HFCs arise due to the simultaneous effects of inbreeding on
86 variation among individuals in marker heterozygosity and fitness (David *et al.* 1995; David 1998; Bierne
87 *et al.* 2000; Hansson & Westerberg 2002). Specifically, inbreeding affects the genome including the panel
88 of genetic markers by increasing the proportion of loci that are IBD and by causing ID. When the aim of a
89 study is to infer the effects of inbreeding on fitness from a panel of genetic markers, two related questions
90 arise: (1) How well does MLH at genetic markers reflect IBD_G ? and (2) How large is the inbreeding load,
91 i.e. the correlation between inbreeding and fitness? These questions led to the development of a model
92 to estimate these relationships based on the inbreeding coefficient f defined as individual IBD_G (Bierne
93 *et al.* 2000). This model was developed further to estimate how well marker heterozygosity reflects F_P ,
94 which itself is an imprecise measure of IBD_G , but the best that existed in pre-genomic times (Slate *et al.*
95 2004). Within this framework, Szulkin *et al.* (2010) used g_2 (David *et al.* 2007), a point estimate of
96 ID, to measure $\sigma^2(IBD_G)$. This allows the derivation of formulas to estimate the correlations between

97 inbreeding, MLH and fitness purely from a set of genetic markers.

98 **Quantifying effects of inbreeding on heterozygosity and fitness**

99 The general effect model assumes that heterozygosity at genetic markers (h , here defined as standardised
100 MLH, Coltman *et al.* 1999) is correlated with genomic heterozygosity through variation in individual
101 inbreeding levels (f) and that individual fitness (W) declines as a linear function of f which is expected
102 if deleterious mutations have non-epistatic effects (Bierne *et al.* 2000). In other words, the correlation
103 between W and h arises through the simultaneous effects of inbreeding level on fitness ($r(W, f)$) and
104 marker heterozygosity ($r(h, f)$) (Bierne *et al.* 2000; Slate *et al.* 2004; Szulkin *et al.* 2010).

$$r(W, h) = r(h, f) r(W, f) \quad (\text{eqn 1})$$

105

106 Although F_P has been used as a measure of f in the above formula (Slate *et al.* 2004; Szulkin *et al.*
107 2010), here we define the inbreeding coefficient f as a variable that explains all of the variance in genomic
108 heterozygosity ($\sigma^2(IBM_G)$) and therefore includes both variance depending on an individual's pedigree
109 and the degree of linkage among loci (Bierne *et al.* 2000). When it is not possible to directly measure an
110 individual's inbreeding level f , we can use ID to characterize the distribution of f in a population. A
111 measure of ID that can be related to HFC theory is g_2 (David *et al.* 2007), which quantifies the extent
112 to which heterozygosities are correlated across pairs of loci (see Appendix S1 for details). Based on g_2
113 as an estimate of ID, it is then possible to calculate the expected correlation between h and inbreeding
114 level f as follows (Szulkin *et al.* 2010):

$$r^2(h, f) = \frac{g_2}{\sigma^2(h)} \quad (\text{eqn 2})$$

115 Finally, the expected squared correlation between a fitness trait W and inbreeding level f can be derived
116 by rearranging eqn 1 (Szulkin *et al.* 2010):

$$r^2(W, f) = \frac{r^2(W, h)}{r^2(h, f)} \quad (\text{eqn 3})$$

117

118 Software is already available for calculating g_2 from microsatellite datasets (David *et al.* 2007). However,
119 for larger (e.g. SNP) datasets, the original formula is not computationally practical, as it requires a
120 double summation over all pairs of loci. For example, with 15,000 loci, the double summations take of
121 the order of 0.2×10^9 computation steps. For this reason, it is necessary to implement a computationally
122 more feasible formula to calculate g_2 , which assumes that the distribution of true heterozygosity is the

123 same in missing data as in non-missing data, i.e. that the frequency of missing values does not vary
 124 much between pairs of loci (Hoffman *et al.* 2014). In turn, the g_2 parameter builds the foundation for
 125 the implementation of the above framework to analyse HFCs, which is recommended to be routinely
 126 computed in future HFC studies (Szulkin *et al.* 2010; Kardos *et al.* 2014).

127 The package

128 **inbreedR** is an R package (R Core Team 2015) that provides functions for analysing inbreeding and
 129 HFCs based on microsatellite and SNP data. The main aims of the package are to (i) calculate g_2
 130 and its confidence interval and p -value for both microsatellites and large SNP datasets; (ii) estimate
 131 the influence of inbreeding on marker heterozygosity and fitness through the derivation of $r^2(h, f)$ and
 132 $r^2(W, f)$; and (iii) explore the sensitivity of g_2 and $r^2(h, f)$ to marker number through user friendly
 133 simulations. The overall workflow is shown in Figure 1 and described below. For a more detailed
 134 description of the package and the functions, we have supplied a vignette for the package than can be
 135 accessed via `browseVignettes("inbreedR")` once the package is installed.

136 Example datasets

137 The functionality of **inbreedR** is illustrated using genetic and phenotypic data from an inbred captive
 138 population of oldfield mice (*Peromyscus polionotus*) (Hoffman *et al.* 2014). These mice were paired over
 139 six laboratory generations to produce offspring with F_P ranging from 0 to 0.453. Example files are
 140 provided containing the genotypes of 36 *P. polionotus* individuals at 12 microsatellites and 13,198 SNPs
 141 respectively. Data on body mass at weaning, a fitness proxy, are also available for the same individuals.

```
library(inbreedR)
data("mouse_msats") # microsatellite data, data.frame or matrix
data("mouse_snps") # snp data, data.frame or matrix
data("bodyweight") # fitness data, numeric vector
```

142 Data conversion and checking

143 The working format of **inbreedR** is an *individual x loci matrix* or `data.frame` in which rows represent
 144 individuals and each column represents a locus. If an individual is heterozygous at a given locus, it
 145 is coded as 1, whereas a homozygote is coded as 0, and missing data are coded as NA. We provide a
 146 converter function from a common two-column-per-locus (allelic) format to the working format, as well
 147 as a function to check for common formatting errors within the input matrix. Guidelines for extracting
 148 genotype data from VCF files are given in the vignette.

```

# transforms microsatellite data into (0/1)
mouse_microsats <- convert_raw(mouse_msats)
# checks the data
check_data(mouse_microsats, num_ind=36, num_loci=12)
#> [1] TRUE
check_data(mouse_snps, num_ind=36, num_loci=13198)
#> [1] TRUE

```

149 Identity disequilibrium

150 The package provides functions to calculate g_2 for both microsatellites and SNPs. The `g2_microsats()`
 151 function implements the formula given in David *et al.* (2007). For large datasets (e.g. SNPs) the
 152 `g2_snps()` function implements a computationally feasible formula described in Appendix S1. For both
 153 microsatellites and SNPs, `inbreedR` also calculates confidence intervals by bootstrapping over individuals
 154 (Table 1). It also permutes the genetic data to generate a p -value for the null hypothesis of no variance
 155 in inbreeding in the sample (i.e. $g_2 = 0$). The `g2_snps()` function provides an additional argument for
 156 parallelization which distributes bootstrapping and permutation across cores.

```

g2_mouse_microsats <- g2_microsats(mouse_microsats, nperm=1000, nboot=1000, CI=0.95)
g2_mouse_snps <- g2_snps(mouse_snps, nperm=100, nboot=100, CI=0.95, parallel=FALSE, ncores=NULL)

```

157 The results of both functions can be plotted as histograms with CIs (Figure 2).

```

par(mfrow=c(1,2))
plot(g2_mouse_microsats, main = "Microsatellites", col = "cornflowerblue", cex.axis=0.85)
plot(g2_mouse_snps, main = "SNPs", col = "darkgoldenrod1", cex.axis=0.85)

```

158 Another approach for estimating ID is to divide the marker panel into two random subsets, compute the
 159 correlation in heterozygosity between the two, and repeat this hundreds or thousands of times in order to
 160 obtain a distribution of heterozygosity-heterozygosity correlation coefficients (Balloux *et al.* 2004). This
 161 approach is intuitive and has been shown to be equivalent to g_2 in its power to detect non-zero variance in
 162 inbreeding (Kardos *et al.* 2014) although it can be criticised on the grounds that samples within the HHC
 163 distribution are non-independent. Moreover, g_2 is preferable because it directly relates to HFC theory
 164 (eqn 2). The `HHC()` function in `inbreedR` calculates HHCs together with confidence intervals, specifying
 165 how often the dataset is randomly split into two halves with the `reps` argument.

```

HHC_mouse_microsats <- HHC(mouse_microsats, reps=1000)
HHC_mouse_snps <- HHC(mouse_snps, reps=100)

```

166 The results can be outputted as text (Table 2) or plotted as histograms with CIs (Figure 3).

```

par(mfrow=c(1,2))
plot(HHC_mouse_microsats, main = "Microsatellites", col = "cornflowerblue", cex.axis=0.85)
plot(HHC_mouse_snps, main = "SNPs", col = "darkgoldenrod1", cex.axis=0.85)

```

167 HFC parameters

168 Assuming that HFCs are due to inbreeding depression, it is possible to calculate both the expected
 169 correlation between heterozygosity and inbreeding level ($r^2(h, f)$) and the expected correlation between
 170 a fitness trait and inbreeding ($r^2(W, f)$) as described in eqn 1. These calculations are implemented in
 171 **inbreedR** using the functions `r2_hf()` and `r2_Wf()`. Both functions include an `nboot` argument to run
 172 bootstrapping over individuals and estimate confidence intervals. Similar to the base R `glm()` function,
 173 the distribution of the fitness trait can be specified using the `family` argument, as shown below:

```

# r^2 between inbreeding and heterozygosity
hf <- r2_hf(genotypes = mouse_microsats, nboot = 100, type = "msats")
# r^2 between inbreeding and fitness
Wf <- r2_Wf(genotypes = mouse_microsats, trait = bodyweight, family = gaussian, type = "msats", nboot=100)

```

174 Workflow for estimating the impact of inbreeding on fitness using HFC

175 Szulkin *et al.* (2010) in their online Appendix 1 provide a worked example of how to estimate the impact
 176 of inbreeding on fitness within an HFC framework. Below, we show how the required calculations can be
 177 implemented in **inbreedR**. We start with the estimation of identity disequilibrium (g_2) and calculation
 178 of the variance of standardized multilocus heterozygosity ($\sigma^2(h)$), followed by the estimation of the three
 179 correlations from eqn 1. Example code for the microsatellite dataset is shown below and the results for
 180 both microsatellites and SNPs are given in Table 3.

```

# g2 and bootstraps to estimate CI
g2 <- g2_microsats(mouse_microsats, nboot = 1000)
# calculate sMLH
het <- sMLH(mouse_microsats)
# variance in sMLH
het_var <- var(het)
# Linear model
mod <- lm(bodyweight ~ het)
# regression slope
beta <- coef(mod)[2]
# r^2 between fitness and heterozygosity
Wh <- cor(bodyweight, predict(mod))^2
# r^2 between inbreeding and sMLH including bootstraps to estimate CI
hf <- r2_hf(genotypes = mouse_microsats, type = "msats", nboot = 1000)
# r^2 between inbreeding and fitness including bootstraps to estimate CI
Wf <- r2_Wf(genotypes = mouse_microsats, trait = bodyweight,
            family = gaussian, type = "msats", nboot = 1000)

```

181 Sensitivity to the number of markers

182 Sampling subsets of loci from an empirical genetic dataset and estimation of a statistic of interest based
 183 on these subsets can give insights into the power provided by a given marker panel (Miller *et al.* 2013;
 184 Hoffman *et al.* 2014; Stoffel *et al.* 2015). However, although subsampling markers (with replacement)
 185 from an empirical dataset allows exploration of trends in the magnitude of a statistic, the precision
 186 (variation) of the same statistic is necessarily biased. This is due to the increasing non-independence of
 187 resampled marker sets as they approach the total number of markers. For example, given a dataset of 20
 188 genetic markers, repeatedly subsampling 18 markers and calculating g_2 will always lead to lower variation
 189 in the estimates than subsampling sets of 5 markers. To circumvent this problem, the `simulate_g2()`
 190 function simulates genotypes from which subsets of loci can be sampled independently. The simulations
 191 can be used to evaluate the effects of the number of individuals and loci on the precision and magnitude
 192 of g_2 . The user specifies the number of simulated individuals (`n_ind`), the subsets of loci (`subsets`)
 193 to be drawn, the heterozygosity of non-inbred individuals (`H_nonInb`, i.e. expected heterozygosity in
 194 the base population) and the distribution of f among the simulated individuals. The f values of the
 195 simulated individuals are sampled randomly from a beta distribution with mean (`meanF`) and variance
 196 (`varF`) specified by the user (e.g. as in Wang 2011). This enables the simulation to mimic populations
 197 with known inbreeding characteristics or to simulate hypothetical scenarios of interest. For computational
 198 simplicity, allele frequencies are assumed to be constant across all loci and the simulated loci are unlinked.
 199 Genotypes (i.e. heterozygosity/homozygosity at each locus) are assigned stochastically based on the f
 200 values of the simulated individuals. Specifically, the probability of an individual being heterozygous at
 201 any given locus (H) is expressed as $H = H_0(1 - f)$, where H_0 is the user-specified heterozygosity of a
 202 non-inbred individual and f is an individual's inbreeding coefficient drawn from the beta distribution.

```

sim_g2_mouse_microsats <- simulate_g2(n_ind = 50, H_nonInb = 0.5, meanF = 0.2, varF = 0.03,
                                     subsets = c(5, 10, 15, 20, 25, 30, 35, 40, 45, 50),
                                     reps = 100, type = "msats")

sim_g2_mouse_snps <- simulate_g2(n_ind = 50, H_nonInb = 0.5, meanF = 0.2, varF = 0.03,
                                 subsets = seq(from = 1000, to = 10000, by = 1000),
                                 reps = 100, type = "snps")

```

203 The results can be visualized by showing the mean and CI of g_2 plotted against the number of loci used
 204 (Figure 4). Bear in mind that g_2 values calculated from the simulated data may over-estimate precision
 205 due to the assumption of unlinked loci. However, in practice, the number of linked SNPs in most real

206 datasets will be small compared to the number of unlinked SNPs (Szulkin *et al.* 2010) and hence g_2 should
 207 not be substantially affected.

```
par(mfrow = c(1, 2), mar=c(5,5.15,3,1.2))
plot(sim_g2_mouse_microsats, main = "Microsatellites",
     cex.axis=1.5, cex.main = 1.5, cex.lab = 1.5)
plot(sim_g2_mouse_snps, main = "SNPs",
     cex.axis=1.5, cex.main = 1.5, cex.lab = 1.5)
```

208 Finally, it is of interest to infer how well genetic marker heterozygosity reflects the inbreeding level f and
 209 whether this correlation could be increased by genotyping individuals at a larger set of markers. The
 210 `simulate_r2_hf()` function can be used to compare the precision and magnitude of the expected
 211 squared correlation between heterozygosity and inbreeding ($r^2(h, f)$) for a given number of genetic
 212 markers.

```
sim_r2_mouse_microsats <- simulate_r2_hf(n_ind = 50, H_nonInb = 0.5, meanF = 0.2, varF = 0.03,
                                       subsets = c(5, 10, 15, 20, 25, 30, 35, 40, 45, 50),
                                       reps = 100, type = "msats")

sim_r2_mouse_snps <- simulate_r2_hf(n_ind = 50, H_nonInb = 0.5, meanF = 0.2, varF = 0.03,
                                   subsets = seq(from = 1000, to = 10000, by = 1000),
                                   reps = 100, type = "snps")
```

213 The results can again be plotted as a series of $r^2(h, f)$ estimates together with their means and CIs
 214 (Figure 5).

```
par(mfrow = c(1, 2), mar=c(5,5.15,3,1.2))
plot(sim_r2_mouse_microsats, main = "Microsatellites",
     cex.axis=1.5, cex.main = 1.5, cex.lab = 1.5)
plot(sim_r2_mouse_snps, main = "SNPs", cex.axis=1.5,
     cex.main = 1.5, cex.lab = 1.5)
```

215 Effects of LD under the general effect model

216 LD may affect the strength of an HFC because it increases $\sigma^2(IBD_G)$ (Bierne *et al.* 2000). This is
 217 because the variance in individual IBD_G is explained by (i) a component that reflects the different
 218 pedigrees of individuals, and (ii) a component that reflects variation among individuals with the same
 219 pedigree (Bierne *et al.* 2000). In the absence of linkage (i.e. if there were infinitely many unlinked loci),
 220 an individual's IBD_G would solely depend on the pedigree. However, loci do not segregate independently
 221 and LD and especially physical linkage will therefore cause variation in IBD_G among individuals with the
 222 same pedigree. Calculating g_2 and derived HFC statistics based on large SNP datasets, which are likely
 223 to include linked markers, is therefore not a problem *per se*. As g_2 does not incorporate any pedigree

information but purely quantifies correlated heterozygosity among genetic marker pairs, it is a direct measure of $\sigma^2(IBD_G)$. The only assumption needed is that IBD is equally frequent among marker loci and fitness loci that are responsible for inbreeding depression. Put another way, the fitness loci should have an equivalent genomic distribution to the genetic markers.

Increasing the total number of genetic markers should not affect the proportion of linked markers and should thus not affect g_2 . To test this, we evaluated the sensitivity of g_2 to marker number by repeatedly sampling random subsets of between 100 and 13,000 SNPs from the full mouse dataset and calculating the respective g_2 values. For each subset, markers were sampled without replacement to avoid non-independence, which is why the number of repetitions decreases with increasing marker number. The mean g_2 was found to be stable across all subset sizes, suggesting that, for our dataset, the expected g_2 does not vary appreciably with marker density (Figure 6).

In general, the number of locus pairs in strong linkage is expected to be very low compared to the number of non-linked pairs (Szulkin *et al.* 2010). As g_2 averages over all pairs of loci, this point estimate should therefore be relatively insensitive to the inclusion of linked markers as long as all markers are broadly distributed across the genome. To test this, we conducted LD pruning of our SNP dataset at various stringency thresholds to determine how linkage among SNPs affects g_2 estimates and their confidence intervals. We used the indep-pairphase function in PLINK version 1.09 (Purcell *et al.* 2007) to remove one SNP from each pair with an r^2 above thresholds ranging from 0.5 – 0.99 with increments of 0.05 and a last increment of 0.04. In order to account for our SNPs being on unplaced contigs, we assumed that all SNPs were on the same 'chromosome' and used a sliding window spanning the full dataset. The magnitude and precision of g_2 estimates was found to be stable across all LD pruned datasets (Figure 7), suggesting that, for our dataset, g_2 is relatively insensitive to the inclusion of strongly linked SNPs.

Final remarks

The `inbreedR` package implements a framework to estimate the impact of variation in inbreeding on marker heterozygosity and fitness, which has been suggested to be routinely reported in HFC studies (Szulkin *et al.* 2010; Kardos *et al.* 2014). A good example is a recent study of red deer, in which Huisman *et al.* (2016) quantify identity disequilibria through g_2 in several datasets to estimate the power of a genomic inbreeding measure to detect inbreeding depression. In addition to the quantification of ID and HFCs for empirical data, straightforward simulations within `inbreedR` provide a way to explore the effect of the number of genetic markers on g_2 and the expected correlation between marker heterozygosity and inbreeding. This is important for evaluating the power of a given dataset to measure inbreeding depression, and could also facilitate the planning of future projects by exploring the effects of sample size and marker number on the power to detect ID and HFCs.

257 Although g_2 and related parameters can provide insights into whether an HFC is due to inbreeding or
 258 not, the user should be aware that spurious HFCs can occur due to population structure (Slate *et al.*
 259 2004), which has to be appropriately dealt with beforehand. For instance, genetically distinct populations
 260 could be analysed separately. Also, it is worthwhile considering whether SNPs should be filtered based
 261 on their minor allele frequencies (MAF) prior to analysis. On the one hand, genotyping by sequencing
 262 approaches rely on sufficient depth of coverage to call SNPs with reasonable confidence. Thus, low MAF
 263 SNPs may be disproportionately error prone when the depth of sequence coverage is not high enough to
 264 capture multiple copies of the minor allele. On the other hand, filtering out low MAF SNPs may distort
 265 the allele frequency spectrum and lead to the loss of valuable information (Hoffman *et al.* 2014).
 266 Finally, LD and ID have been seen as alternative hypotheses to explain HFCs (Hansson & Westerberg
 267 2008). However, LD often goes hand in hand with ID and is therefore a relevant variance component
 268 when the aim is to estimate $\sigma^2(IBD_G)$ (Bierne *et al.* 2000; Szulkin *et al.* 2010). As most HFC studies
 269 should be interested in estimating $\sigma^2(IBD_G)$ through g_2 , linked markers need not be pruned as long as
 270 the genomic distributions of the marker and trait loci are comparable. However, if the goal of a study
 271 is to infer characteristics of a pedigree from g_2 (such as self-fertilization rates), it might be useful to
 272 reduce physical linkage among markers using PLINK (Purcell *et al.* 2007) or other methods to ensure
 273 their independence (David *et al.* 2007). Further investigation would be needed to evaluate the impact of
 274 pruning linked markers on selfing or inbreeding rates estimated through g_2 .

275 Computation times

276 Computation times will be negligible for most microsatellite datasets but somewhat longer for very large
 277 SNP datasets. On a standard Laptop (Intel Core I5 2.60GHz, 8 GB RAM) running the `g2_snps()`
 278 function for our example SNP dataset (36 individuals genotyped at 13,198 loci) with 1000 bootstraps
 279 takes 1 min 12 secs without parallelisation and 38 secs with parallelisation on 3 cores. For comparison,
 280 we also simulated a large SNP dataset with 3500 individuals at 37,000 loci (similar to Huisman *et al.*
 281 (2016)) and ran this on a 40 core server with 1000 bootstraps, which took 73 hours.

282 Availability

283 The current stable version of the package requires R 3.2.1 and can be downloaded from CRAN as follows:

```
install.packages("inbreedR")
```

284 In the future, we will aim to extend the functionality of `inbreedR` and the latest development version
 285 can be downloaded from GitHub.

```
install.packages("devtools")
devtools::install_github("mastoffel/inbreedR")
```

286 Data accessibility

287 Both example datasets are included in the R package.

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Table 1. Output of the g_2 functions showing g_2 values and their 95% confidence intervals, standard errors and p-values for 36 mice genotyped at 12 microsatellites and 13,198 SNPs

	\hat{g}_2	CI lower	CI upper	SE	p-value
Microsats	0.022	-0.008	0.065	0.019	0.076
SNPs	0.035	0.022	0.050	0.008	0.010

Table 2. Output of the HHC function, showing mean HHCs with 95% confidence intervals and standard deviations for 36 mice genotyped at 12 microsatellites and 13,198 SNPs.

	Mean	CI lower	CI higher	SD
Microsats	0.194	-0.062	0.453	0.128
SNPs	0.976	0.961	0.987	0.007

Table 3. Parameters central to interpreting HFCs for the microsatellite and SNP datasets. \hat{g}_2 is the empirical point estimate of g_2 , $\hat{\sigma}^2(h)$ is the variance in sMLH, $\hat{\beta}_{Wh}$ is the regression slope of sMLH in a linear model of the fitness trait, \hat{r}_{Wh}^2 is the squared correlation of the fitness trait and sMLH, \hat{r}_{hf}^2 is the expected squared correlation of sMLH and inbreeding and \hat{r}_{Wf}^2 is the expected squared correlation between sMLH and fitness. 95% confidence intervals are shown in squared brackets for the estimates from the package. Note that \hat{r}_{hf}^2 is an expected correlation derived from the ratio of $\hat{g}_2/\hat{\sigma}^2(h)$ and may slightly exceed one due to missing values; we therefore bound the estimate between 0 and 1.

	\hat{g}_2	$\hat{\sigma}^2(h)$	$\hat{\beta}_{Wh}$	\hat{r}_{Wh}^2	\hat{r}_{hf}^2	\hat{r}_{Wf}^2
Microsats	0.022 [-0.01, 0.06]	0.078	1.601	0.121	0.280 [0, 0.52]	0.434 [0, 88]
SNPs	0.035 [0.02, 0.05]	0.033	2.634	0.139	1 [0.89, 1]	0.132 [0, 0.14]

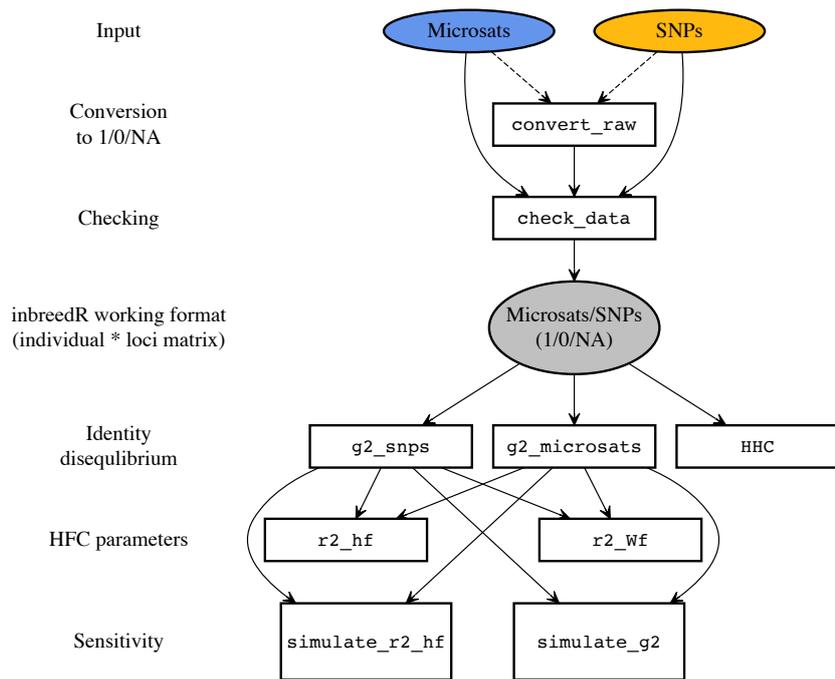


Fig 1. inbreedR workflow. For both microsatellite and SNP datasets, the program provides utilities for data conversion and checking, estimation of identity disequilibrium, derivation of key parameters relating to HFC theory, and exploration of sensitivity to the number of loci deployed. Further details are provided in the main text.

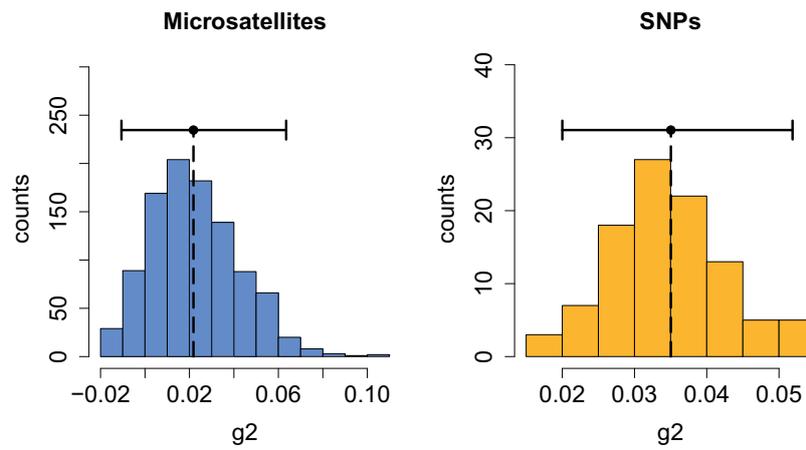


Fig 2. Output of the g_2 functions for the microsatellite and SNP datasets showing the distribution of g_2 estimates from bootstrap samples over individuals together with their 95% CIs. The empirical g_2 estimate is marked as a black dot along the CI.

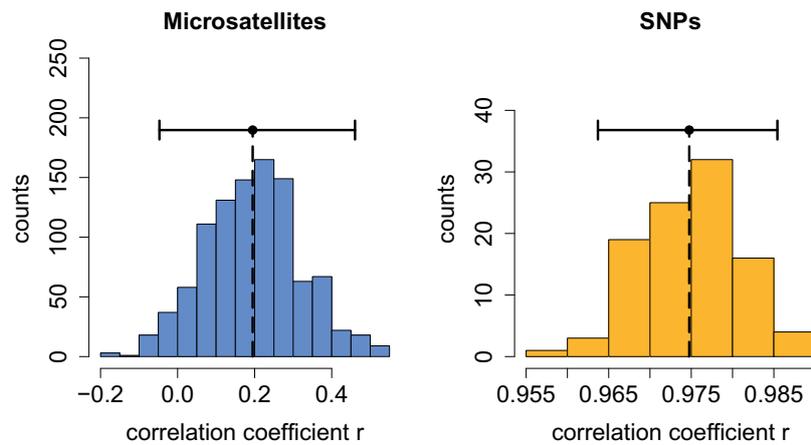


Fig 3. Output of the HHC function showing the distribution of heterozygosity-heterozygosity correlation coefficients for the microsatellite and SNP datasets. Also shown are the mean HHCs as black dots and their 95% CIs. The two distributions are very different, microsatellites being positive but with the 95% CI overlapping zero, and SNPs being well in excess of 0.9 with a much greater precision. This reflects the enhanced power of the larger SNP dataset to capture variance in f among individuals.

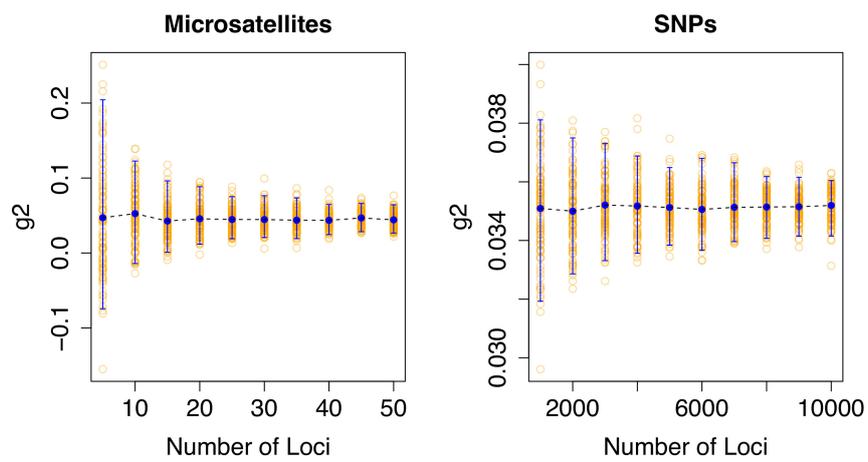


Fig 4. Output of the `simulate_g2()` function. Different sets of microsatellites and SNPs were simulated and stochastically drawn from distributions based on a mean(sd) inbreeding level f of 0.2(0.03) assuming that a non-inbred individual has a heterozygosity of 0.5. The two plots show the g_2 statistics from all samples including their means and 95% CIs.

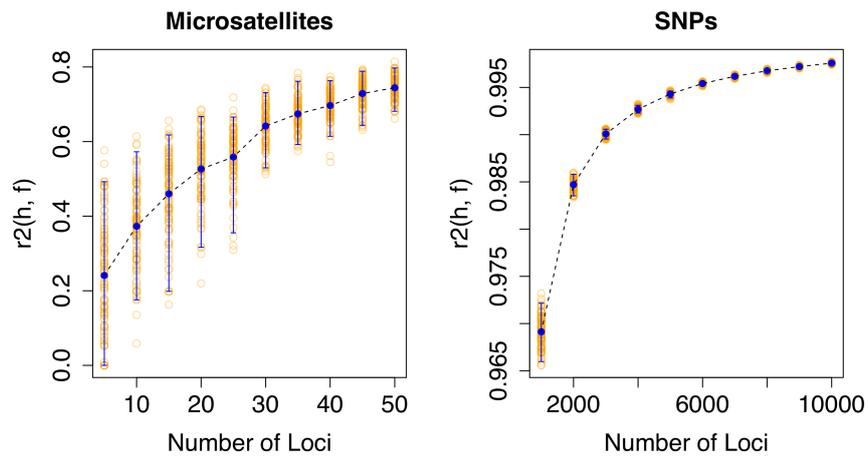


Fig 5. Output of the `simulate_r2_hf()` function. Different sets of microsatellites and SNPs were simulated and stochastically drawn from distributions based on a mean(sd) inbreeding level f of 0.2(0.03) assuming that a non-inbred individual has a heterozygosity of 0.5. The two plots show the $r^2(W, f)$ values for an increasing number of markers including their means and 95% CIs. The expected correlation between inbreeding and marker heterozygosity increases and is estimated with higher precision when the number of markers is increased.

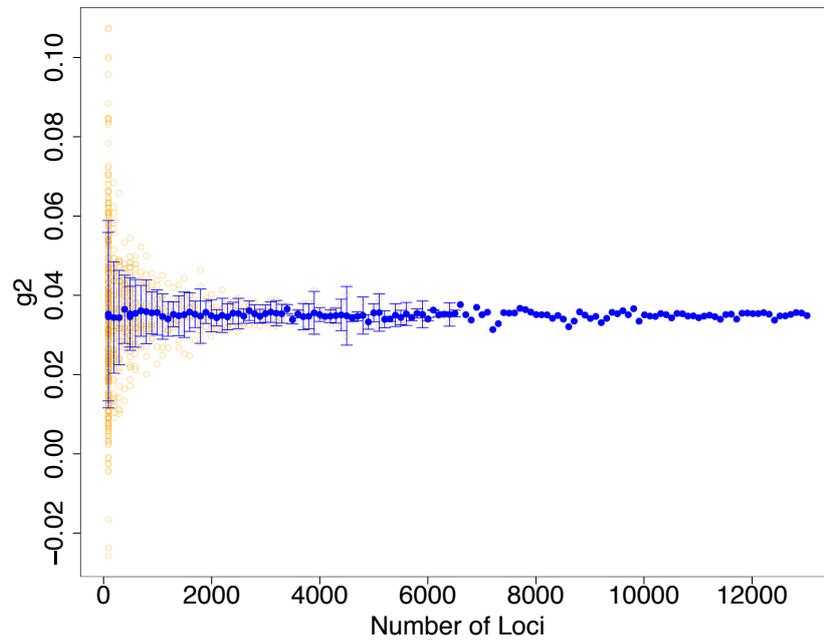


Fig 6. Mean and standard deviation of g_2 derived from an increasing number of SNPs drawn at random from the empirical mouse dataset (13,198 SNPs). The distribution of data points for each subset size is based on sampling without replacement to obtain non-overlapping marker sets. For this reason, the number of datapoints decreases from 131 for 100 markers to 1 for subsets larger than 6599 SNPs. The mean g_2 is stable across all subset sizes, which suggests that estimating g_2 from larger numbers of markers does not introduce bias for our dataset.

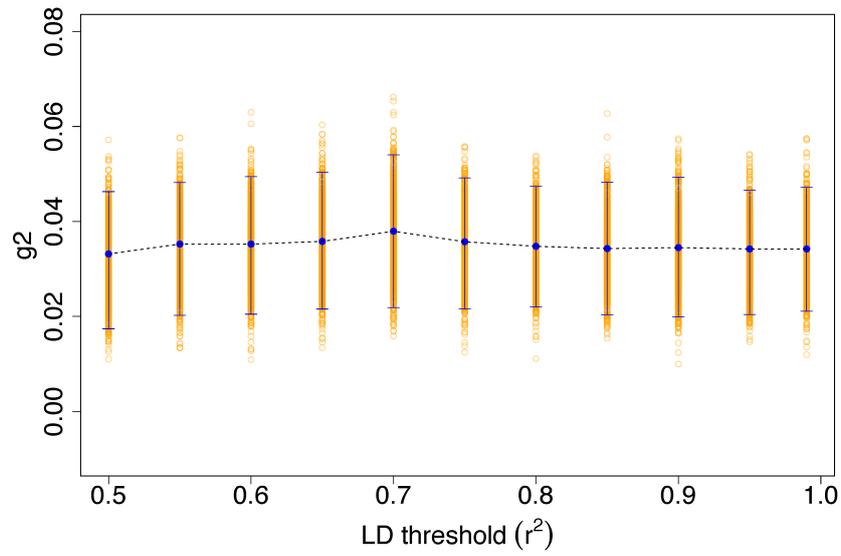


Fig 7. Estimates of g_2 with confidence intervals for subsets of SNPs pruned based on different LD thresholds. We used PLINK to remove one SNP from each marker pair with an r^2 above the respective threshold. As we used a sliding window spanning the full dataset instead of local regions on a chromosome, the retained datasets contained a maximum of 4363 ($r^2 > 0.99$) and a minimum of 1095 ($r^2 > 0.5$) SNPs. The magnitude and precision of g_2 does not vary noticeably for our dataset when pruning strongly linked SNPs.