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Fault Diagnosis of Rolling Bearing using CNN and PCA Fractal Based on Feature Extraction

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Abstract

A novel adaptive decomposition algorithm based on CEEMDAN and fractal dimension is proposed in this study to overcome limitations like redundancy and mode confusion in traditional EMD-based algorithms. An intelligent fault diagnosis model is developed using CNN and the proposed CEEMDAN to enhance rolling bearing state recognition. Sub-signals generated by CEEMDAN are selected and reconstructed using PCA and fractal dimension. In feature extraction and pattern recognition, the proposed Improve Complete Ensemble Empirical Mode Decomposition with Adaptive Noise (ICEEMDAN), coupled with CNN, extracts advanced features from the reconstructed signal for intelligent diagnosis. The methodology is validated through empirical experiments involving rolling bearings, where its superiority and reliability are compared with approaches based on CNN. The accuracy of this method reaches 99.79%

Key Words: complete ensemble empirical mode decomposition with adaptive noise; convolutional neural network; rolling bearing; box dimension; fault diagnosis

1. Introduction

During the explosive development of computer and sensor technology over the years, rotating equipment malfunction monitoring and diagnosis has facilitated the emergence of enormous and high-dimensional big data [1-2]. Energy security and environmental conservation are becoming increasingly essential worldwide, while the quick development of new energy sources such as wind, water, and nuclear energy needs the utilization of effective and reliable rotating equipment [3]. However, rolling bearing of rotating equipment is the most fundamental and susceptible fundamental component, and its steady and efficient operation is closely associated to the overall performance of energy extraction equipment [4-6]. Meanwhile, its vibration signals are not only solely handy to collect, but also rich in a giant quantity of superb fault information. It has become as the preferred signal to analyze the fault traits of rolling bearings, which can also effectively minimize the downtime and useless maintenance triggered caused by equipment failure and lengthen the service life of equipment [7-9]. Therefore, the predominant focal point have to be on rolling bearing situation monitoring and fault diagnosis. The irregular vibration and implications of the device in the actual work setting can easily cause the typical nonlinear and nonstationary characteristics that appear when collecting signal by acceleration sensors, and it is also difficult to guarantee the purity of the signal, posing a serious challenge to effective the features extraction and timely fault warning [10]. The early fault diagnosis process is mainly divided signal acquisition, extraction of fault features, identification and classification, among which the feature extraction is the most critical process in preprocessing [11].

In order to effectively accomplish fault diagnosis tasks in the presence of noise interference, vibration signals must be preprocessed to decrease noise in order to extract fault features of signal more effectively. Time-frequency analysis has recently been popular in the field of fault detection, as it can successfully identify fault features from nonlinear signals under noise, allowing for improved mechanical equipment preventive and maintenance [12-13]. A large number of studies have been carried out by many scholars, Gabor [14] proposed the short-time Fourier

42 transform (STFT), which uses a time-frequency representation to obtain the power spectrum at different times by
43 moving the window function to realize fault analysis. Considering the relation of frequency and time resolution,
44 Morlet [15] proposed the wavelet transform, a time-frequency local transform algorithm that receives and expands
45 the localization idea of the STFT.

46 In order to address the issue of limited adaptability arising from the manual configuration requirement for
47 wavelet transform metrics such as wavelet basis and decomposition layers in the aforementioned methods .Huang
48 et al [16] was the one to propose the empirical mode decomposition (EMD) approach, which can deconstruct an
49 extremely complex noisy signal into a series of intrinsic modal functions (IMFs) without requiring human
50 interaction. Despite its widespread application in the fields of electrocardiogram (ECG) image processing [17],
51 signal filtering [18] and rotating machinery fault diagnosis [19] etc. The EMD was later discovered to have mode
52 aliasing, which has a direct impact on fault diagnostic precision [20].

53 In order to address the issue of mode aliasing inherent in EMD, Wu and Huang [21] proposed the ensemble
54 empirical mode decomposition (EEMD), which may retain data continuity and suppress mode aliasing by adding
55 white noise to the input signal for EMD. Furthermore, the consequences of a couple of decomposition are averaged
56 to attain the last IMF. Despite the fact that this method has been applied to diagnose rotating machinery faults by
57 the domestic and international scholars[22-24], adding white noise to the raw signal repeatedly via the EEMD
58 method will result in reconstruction errors. YEH [25] presented the complete EEMD (CEEMD) as a key upgrade to
59 EEMD. The CEEMD algorithm can makes sure decomposition accuracy and successfully eliminates residual white
60 noise in the rebuilt signal decomposing the time domain signal by adding the two opposite white noise. Both
61 EEMD and CEEMD, however, generally require a significant amount of computing, and the decomposition is
62 overly reliant on the amplitude of adding white noise and the times of ensemble average [26].

63 In order to address the computational intensity and the excessive reliance on the amplitude of added white
64 noise and the number of ensemble averages in both EEMD and CEEMD decomposition processes. Improved
65 versions of the CEEMD analysis have been developed to overcome the problem of inefficiency, culminating in the
66 Complete Ensemble Empirical Mode Decomposition with Adaptive Noise (CEEMDAN) [27]. At each level of
67 EMD decomposition, the CEEMDAN adds adaptive white noise and calculates the residual signal to obtain IMF.
68 Furthermore, the decomposition process is comprehensive, and the reconstruction error is relatively tiny regardless
69 of the number of integration times [28]. Moreover, Smith [29] devised the local mean decomposition (LMD)
70 approach, which used the slider mean instead of cubic spline interpolated in EMD but had the similar terminal
71 effect. Eventually, the CEEMDAN method is utilized to filter and extract defect feature information from rolling
72 bearings in this work, outperforming the above traditional modal decomposition strategy.

73 Precise and reliable extraction of faults signal data is an important factor of fault detection and diagnosis, and
74 it has a direct impact on fault diagnostic recognition rate. Although the time-frequency decomposition method is an
75 effective modal decomposition, precisely selecting the modal components with fault features is problematic.
76 Furthermore, the extracted initial feature components have a high dimension and may contain redundant or
77 insensitive information, adding to the calculation's complexity.

78 In order to effectively reduce data dimensionality and computational complexity while avoiding dimension
79 disasters. In 1901, Karl Pearson created PCA algorithm which is one of the most extensively used data dimension
80 reduction algorithms today [30]. WANG et al. [31] used PCA algorithm to recognize bearing faults. It can reduce
81 the number of variables in regression and clustering techniques by extracting the largest individual differences from
82 the principal components and reduce the dimension of feature vectors drawn from raw vibration signals, improving
83 real-time performance and fault diagnosis accuracy. This technique has been utilized by several researchers to

84 diagnose rotating machine faults [32-36]. Although the studies above can effectively minimize the complexity of
85 data dimension and calculation and avoid dimensional disasters, they all overlook a critical issue: fault information
86 is not included in a single IMF component, but rather in a number of them.

87 In order to address the issue of fault information being distributed across multiple IMF components. The
88 fractal dimension proposed by Mandelbrot in 1975 not only better describes the complexity and nonlinear
89 characteristics of vibration signals, but it also has good anti-noise and relatively simple calculation, making fault
90 information pleasant to showcase and improving fault identification performance and generalization ability [37].

91 In order to address the issue of spurious, redundant, and pseudo components encountered during the
92 CEEMDAN algorithm's processing of nonlinear vibration signals, The application of PCA for the purpose of
93 filtering IMF components is an effective method for mitigating redundancy within the context of processing
94 nonlinear vibration signals[38-39]. We propose a pre-processing filter approach that fractal box dimension
95 combines PCA algorithm.

96 After selecting low-dimensional sensitive fault feature components for reconstruction, a suitable fault
97 diagnosis approach is used to identify and classify the different types of bearing states. [40]. Traditional defect
98 diagnostic approaches are primarily data-driven and relied on mechanism models. The mechanism model diagnosis
99 approach necessitates the development of a comprehensive mathematical model, therefore its application breadth is
100 limited. The data driver does not need to create a mathematical model; instead, it depends on an expert system or a
101 fault library to perform problem diagnostics [41-42]. Although the approaches listed above have a high fault
102 detection rate, they all require a shallow learning algorithm to recognize fault diagnosis since they cannot learn
103 their own characteristics, self-adaptive fault feature extraction, and weak model generalization. Convolutional
104 neural networks are one of the most prominent deep learning models, capable of combining feature extraction with
105 state categorization. Furthermore, its convolutional kernel can adaptively train and extract fault features in signals,
106 avoiding the error of artificial feature extraction and selection, and improving fault diagnostic accuracy. It's also
107 been commonly used in the industrial industry [43-46]. The results show that CNN is not only capable of digesting
108 large amounts of high-dimensional data, but also of self-learning. However, it is still not possible to exclude
109 external noise interfering with defect diagnostics. A new rolling bearing fault diagnosis approach based on
110 ICEEMDAN fusion deep learning is presented for these reasons. The following are the article's primary
111 contributions and superiorities:

112 (i) We proposed ICEEMDAN method to solve the limitations in EMD、EEMD or CEEMDAN algorithm for
113 dealing with unstable signals.

114 (ii) We proposed a new signal fusion method for IMF modes reconstruction based on PCA algorithm and
115 fractal box dimension.

116 (iii) We developed an intelligent ICEEMDAN-CNN model for fault diagnosis, which combining with the
117 advantages of filter.

118 The rest of the paper is laid out in the following states. Section 2 discusses the strategies for recognizing states
119 and preprocessing. Section 3 describes the new structure of the ICEEMDAN-CNN model framework. Section 4
120 presents the test experimental data as well as the validation of the ICEEMDAN-CNN approach. Section 5 wraps off
121 with the findings.

122 **2. The relevant theory of state recognition and preprocessing**

123 **2.1 CEEMDAN algorithm**

124 CEEMDAN is the ultimate improved algorithm based on Torres' EMD [47]. Using adaptive white noise, it is

125 possible to successfully eliminate modal aliasing, redundant and false components. It also avoids the need to
 126 compute the various order components. The specific procedural steps of CEEMDAN encompass the following
 127 sequence: initially, introducing adaptive white noise into the original signal; subsequently, decomposing the signal.
 128 For each IMF component, employing a collective averaging method, iteratively repeating the process of
 129 decomposition and noise introduction to further enhance the precision and stability of the decomposition. Lastly,
 130 amalgamating all the processed IMF components culminates in the ultimate CEEMDAN decomposition result. The
 131 CEEMDAN decomposition steps are shown in Fig.1.

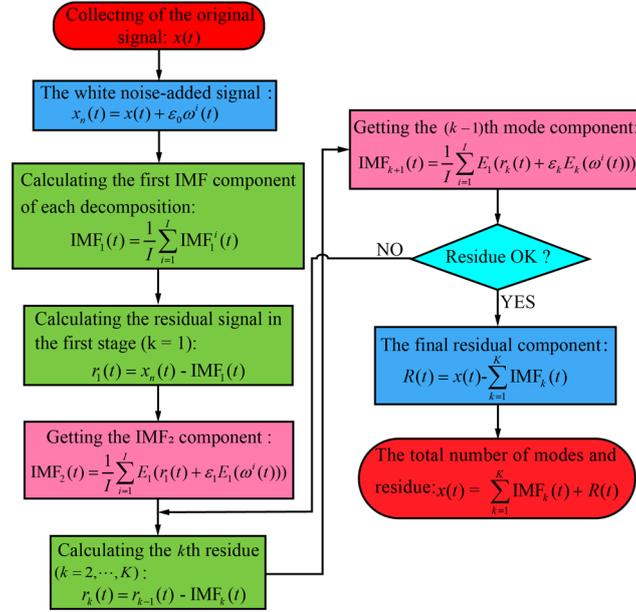


Fig.1 The flow chart of CEEMDAN

132 where $E_i(\cdot)$ is the k th IMF decomposed by the EMD, $\omega^j(t), (i=1, \dots, I)$ is the added white noise, I is the number of
 133 times to add white noise.
 134

135 2.2 Principal component analysis

136 Principal component analysis is a method for preparing high-dimensional feature data. It can keep the most
 137 critical elements of high-dimensional data while removing complex noise and unexpected characteristics in order to
 138 improve data processing performance. As a result, PCA has been widely employed in exploratory data analysis and
 139 the development of prediction models. It is widely used to reduce dimensionality through trying to project each data
 140 point onto only the first few principal components to get lower-dimensional data while retaining as much of the
 141 data's variation as feasible [48]. The steps of PCA [49] as follows:

142 Step 1: Normalize the original feature space data $X = \{x_1, x_2, x_3, \dots, x_n\}$ to get standardized X^* .

143 Step 2: Calculate the covariance matrix $\text{cov}(X^*)$.

144 Step 3: Using eigenvalue decomposition to calculate the eigenvalues and eigenvectors of covariance
 145 matrix $\text{cov}(X^*)$.

146 Step 4: Ordering eigenvalue and Choosing components and forming a feature vector.

147 Step 5: Transform the data into a new space constructed by feature vectors.

148 2.3 Fractal theory

149 The original meaning of fractal is irregular, fractional, and fragmented things, which can be regarded as the
 150 similarity between the part and the whole in some ways [50]. Fractal dimension is a useful metric for measuring

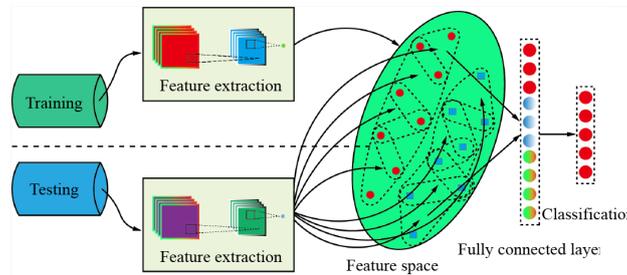
151 fractals, as it accurately describes the complexity and nonlinearity of vibration signals [51]. Although there are a
 152 variety of fractal dimensions that can be used to describe the complexity of signals, such as Hausdorff dimension,
 153 box dimension, capacity dimension, information dimension, correlation dimension, etc. The box dimension is now
 154 the most widely used because of its simple and efficient calculation [52]. As a result, it is preferred among
 155 nonlinear field researchers [53-55]. The definition of fractal box dimension is Eq. (1) [35].

$$D_B = \lim_{\varepsilon \rightarrow 0} \frac{\ln N(\varepsilon)}{\ln(1/\varepsilon)} \quad (1)$$

156 where $Y \subset R^n, Y \neq \Phi$, if there $N(\varepsilon)$ hypercube can cover Y .

157 2.4 CNN Classification Model

158 Convolutional neural network is derived from the neurons of primate visual nervous system. It not only has
 159 neural network with deep structure, but also has powerful data mining and feature extraction capabilities [56].
 160 Local receptive field weight sharing and down-sampling, as its unique features, can not only realize the deep
 161 mining of data features, but also enhance the self-learning ability of data features, eliminating algorithm overfitting
 162 well [57]. The CNN model structure is shown in Fig.2.



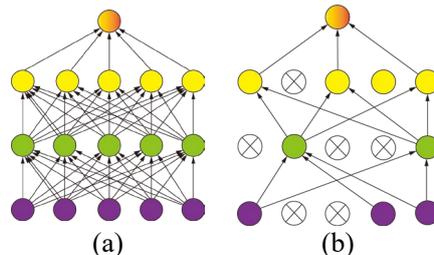
163 Fig.2 The model structure of CNN

164 2.4.1. Convolutional and Pooling layer

165 The convolutional layer is the CNN core, which uses the product and reconstruction of corresponding regions
 166 overlapped by the convolutional kernel and the input features, and achieves feature information extraction by
 167 adding bias to obtain the feature values. Although the feature information extraction ability is improved through the
 168 convolutional layer, the dimension of data is increased, resulting dimension disaster. However, the pooling layer
 169 can reduce the number of parameters while retaining its key features to achieve the purpose of reducing and
 170 screening the main features [58].

171 2.4.2. Fully connected layer and Dropout

172 The full connection layer can classify feature information effectively, and the hidden layer of multi-layer
 173 perceptron can better integrate the data information after convolutional pooling [59]. The regularization technique
 174 of Dropout can omit some elements of the hidden layer to prevent overfitting and improve the generalization
 175 performance of the model [60]. The effect schematic diagram of Dropout operation is shown in Fig.3.



176 Fig.3 The effect schematic diagram of Dropout operation: (a) Fully connected network of standard; (b)The net
 177 after Dropout

178 **3. The proposed ICEEMDAN-CNN model architecture structure**

179 **3.1 ICEEMDAN algorithm**

180 Although the CEEMDAN algorithm with adaptive adding white noise can effectively reduce the mode aliasing
 181 problem, it still cannot completely eliminate the influence of redundant components and false components, which
 182 interferes with the selection of principal components. However, Pearson correlation coefficient, kurtosis and grey
 183 correlation have been used to screen the optimal IMF components by a large number of scholars [61-62-63-64].
 184 However, they all ignore the fault information often exists in some IMF components, which makes it difficult to
 185 extract all effective information completely. In this paper, the combine method of PCA and fractal dimension is
 186 used to improve CEEMDAN. PCA can extract effective fault information by dimensionality reduction of data, and
 187 use cross analysis method to calculate the fractal dimension before and after dimensionality reduction to reconstruct
 188 the optimal component group. According to the fractal theory, the fractal dimension has a positive correlation with
 189 the signal stability. The flow chart of the improved CEEMDAN algorithm is shown in Fig.4.

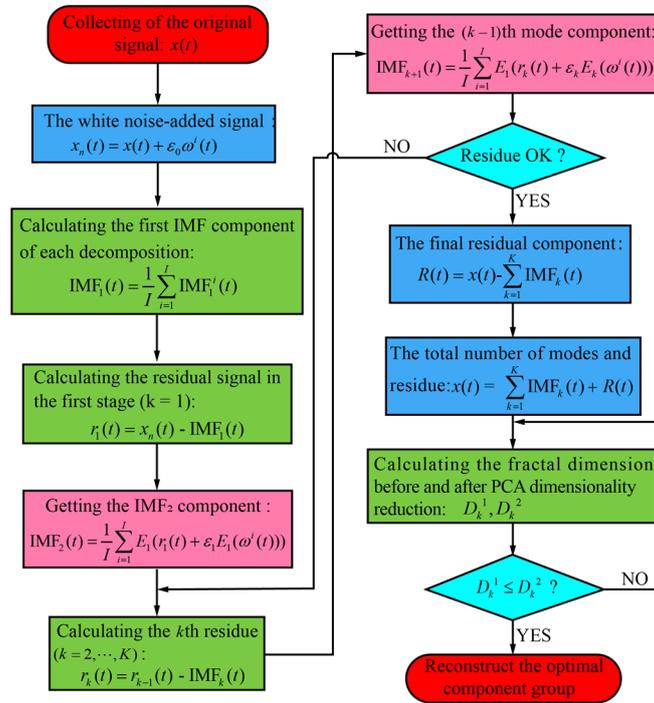


Fig.4 The improved CEEMDAN flow chart

190 **3.2 ICEEMDAN model architecture**

191 The ICEEMDAN-CNN model architecture proposed in this paper consists of CEEMMDAN decomposition
 192 denoising, PCA dimensionality reduction processing, fractal dimension screening fault feature component
 193 reconstruction group, feature learning layer and classification layer of one-dimensional CNN. Figure 5 shows the
 194 proposed ICEEMDAN-CNN model framework structure.

195 As shown in Fig. 5, the proposed method is divided into two steps altogether: model training and verification.
 196 The collected vibration signals need to be decomposed by CEEMDAN, avoiding effectively endpoint effect and
 197 reducing redundant and residual noise in IMF component. Furthermore, PCA method is used to reduce the
 198 dimension of the decomposed high-dimensional components, which can map the faults that are difficult to identify
 199 to another subspace for dimensionality reduction to extract key feature information and improve the ability of fault
 200 feature extraction. According to the dimension properties of fractal box, the best reconstruction components can be
 201 screened out, eliminating redundant components and false components. Finally, it is input into CNN with powerful

202 data processing advantages to realize accurate identification and classification of faults through the full connection
 203 layer and SOFTMAX.

204 The structural parameters of one-dimensional CNN are shown in detail in Table 1. Compared with the
 205 traditional CNN, Adam gradient descent optimization algorithm is adopted in the proposed model. The CNN is
 206 composed of five convolutional layers and five pooling layers in an alternating fashion, followed by dropout and a
 207 fully connected layer. The learning rate has been maintained at 0.001. The length of one-dimensional signal under
 208 random screening conditions is 2048. Its initial weights are randomly initialized, and the activation function is
 209 ReLU. The cross entropy is the loss function. In addition, multi-layer network structures such as small-size
 210 convolution and pooling, Batch Normalization, and Dropout are used continuously. It can not only simplify the
 211 calculation, avoid gradient explosion, over-fitting and gradient disappearance, but also improve the performance of
 212 fault diagnosis identification and classification [65].

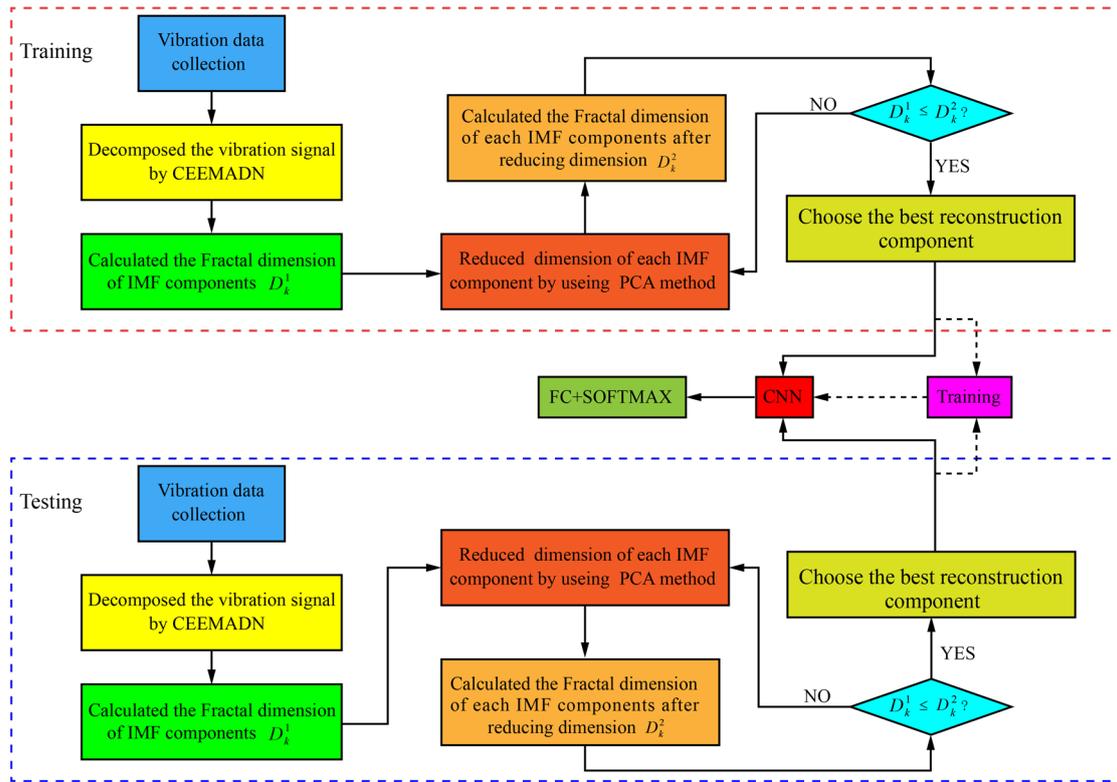


Fig.5 The ICEEMDAN and CNN model architecture

213

Table.1 The parameter of CNN network structure

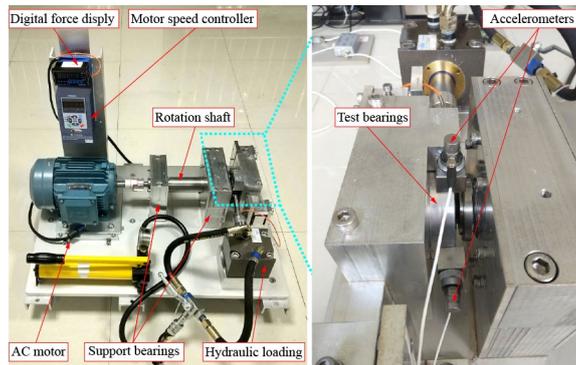
Layer (Type)	Convolution kernels	Step length	Size
Input layer	---	---	1@2048×1
Layer 1	16@11×1	[4 1]	16@510×1
Batch Normalization (BN)	---	---	---
Pooling layer 1	---	[2 1]	16@255×1
Layer 2	32@5×1	[2 1]	32@126×1
Batch Normalization (BN)	---	---	---
Pooling layer 2	---	[2 1]	32@63×1
Layer 3	32@3×1	[1 1]	32@61×1
Batch Normalization (BN)	---	---	---
Pooling layer 3	---	[2 1]	32@30×1

Layer 4	64@2×1	[1 1]	64@29×1
Batch Normalization (BN)	---	---	---
Pooling layer 4	---	[2 1]	64@14×1
Layer 5	128@2×1	[1 1]	128@13×1
Batch Normalization (BN)	---	---	---
Pooling layer 5	---	[1 2]	128@6×1
Dropout (DR)	---	---	128@6×1
Full connection layer	---	---	4@1×1
Softmax	---	---	---

214 **4. Experiments and verification method**

215 **4.1 Sample dataset**

216 For better evaluation of reality and integration with reality, the Xi'an Jiao-tong University experimental data
 217 [66], as the standard bearing vibration data set, is used to examine the performances of three kinds of
 218 decomposition method that include EMD, EEMD and CEEMDAN and to compare the performance with
 219 CNN-based models for proving the superiority of the ICEEMDAN-CNN model. The bearing experimental test
 220 platform is shown in Fig.6. The motor speed of the test platform was 2100 r/min and 2250 r/min, The sensor
 221 utilized is an accelerometer sensor. and the sampling frequency was 25.6 kHz. The sampling duration for each
 222 instance is 1.28 seconds, with a sampling interval of one minute. Consequently, each dataset comprises 32,768 data
 223 points, and a total of 100 datasets were collected for each operational condition. The test conditions [67] are shown
 224 in Table 2.



225 Fig.6 The test platform of bearing

226 Table.2 The test conditions of bearing

Fault types	Mixed damage	Inner ring wear	Cage wear	Outer ring wear
Speed / (r/min)	2100	2250	2250	2250
Radial force / kN	12	11	11	11

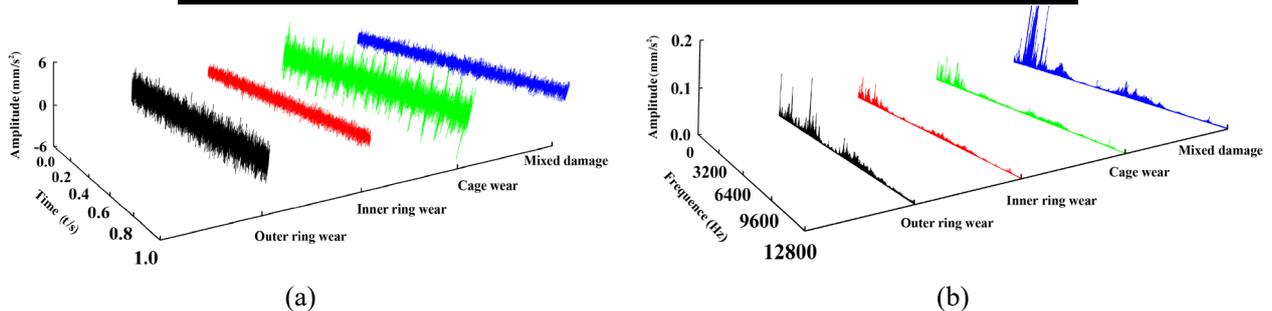


Fig.7 Time and frequency domain waveform of bearing vibration signals: (a) The bearing vibration signal time

domain waveform; (b) The bearing vibration signal frequency domain waveform

227 As can be seen from Table 2, there are four faults of mixed damage, inner ring wear, cage wear and outer ring
228 wear. Their time domain diagram is shown in Fig.7. Although there are some differences in time domain and
229 frequency domain of vibration signals of different faults of rolling bearings, fault identification and classification
230 cannot be carried out directly, so it is more difficult to ensure the diagnosis accuracy. However, the extraction of
231 pure and effective fault features is the basis of diagnosis, so the original signal should be de-noised to highlight the
232 fault information and enhance the practicability of the signal.

233 4.2 Data preprocessing and method analysis

234 In this paper, the original signal was processed by EMD, EEMD and CEEMDAN algorithms respectively to
235 achieve noise reduction. However, there are too much data to display all of them directly. Therefore, only the
236 decomposition results of inner ring wear are shown in Fig. 8. The time domain and frequency domain plots of the
237 three kinds of decomposition results cannot accurately select the best reconstructed component groups for fault
238 analysis. Compared with EMD EEMD algorithm, CEEMDAN algorithm adaptively adds white noise to improve
239 the effect of mode aliasing, but it still can not accurately remove redundant components and false components.

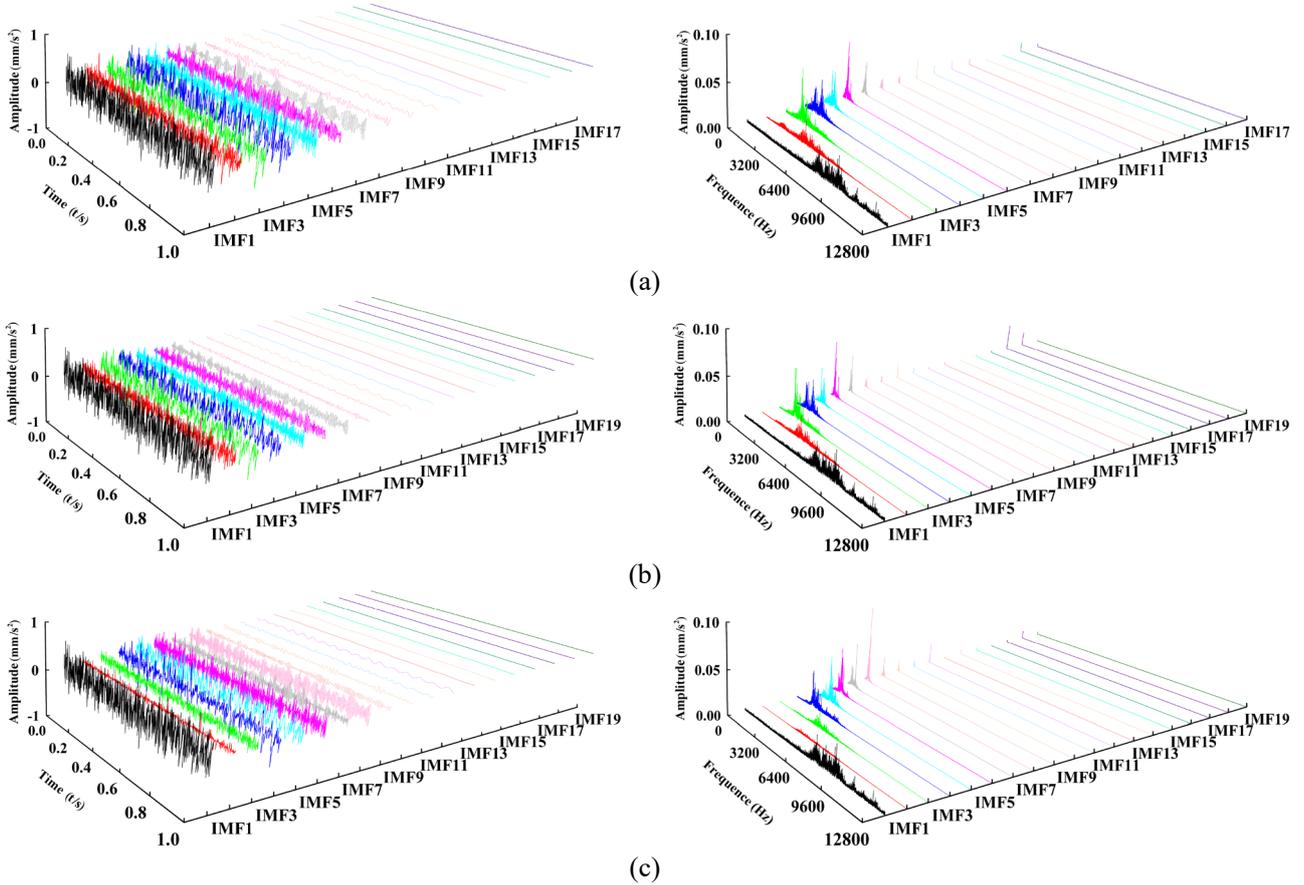


Fig.8 The different decompose of inner ring wear fault signals: (a) The result of EMD decomposed; (b) The result of EEMD decomposed; (c) The result of CEEMDAN decomposed

240 Based on the above problems, this paper proposes a method combining PCA dimension reduction and fractal
241 dimension to screen the best reconstruction components, which can effectively avoid the loss of fault information,
242 eliminate redundant components and improve the identification accuracy of fault diagnosis. Fig.9 shows the
243 comparison results of fractal dimension before and after dimension reduction of four kinds of rolling bearing faults.

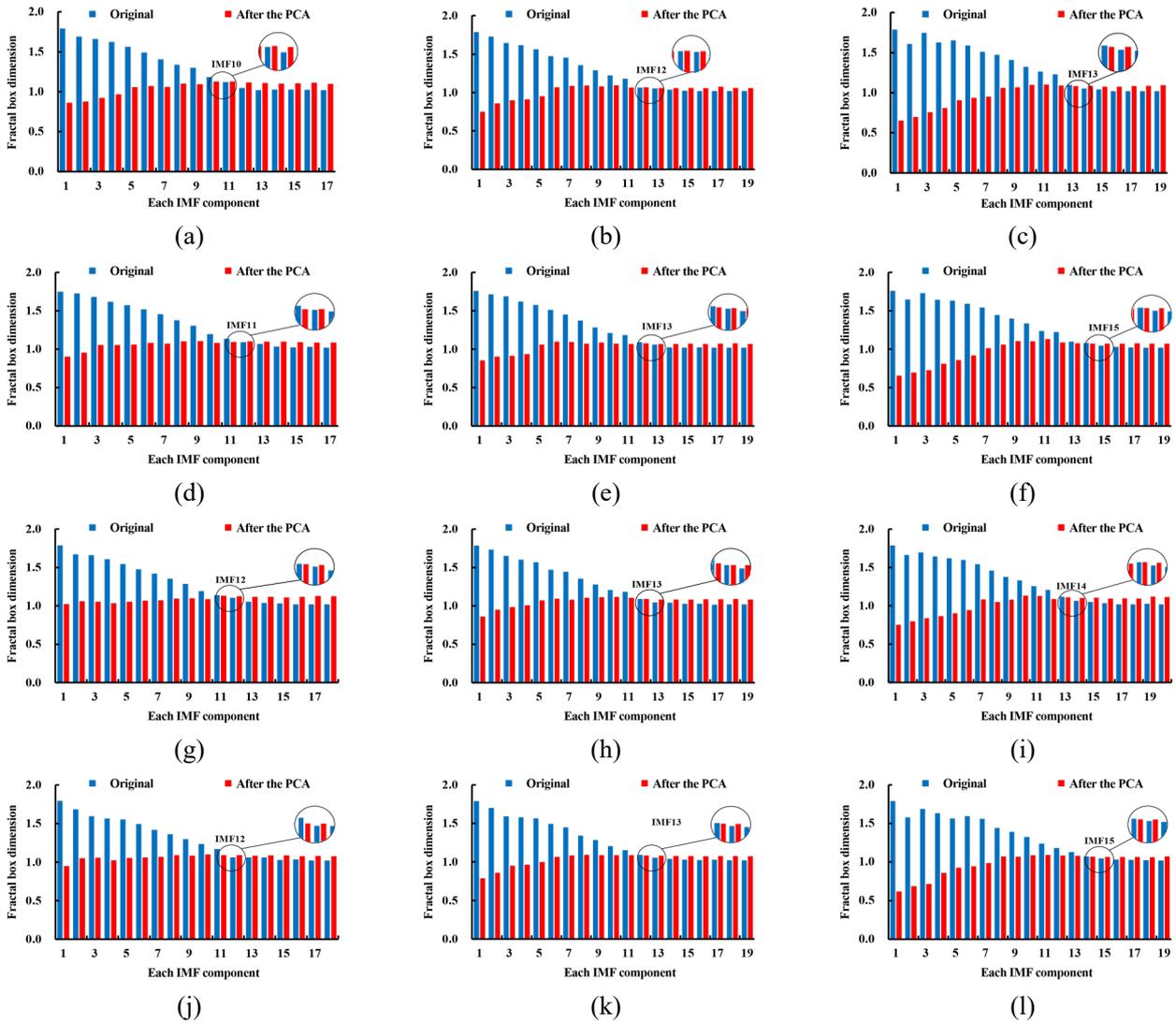
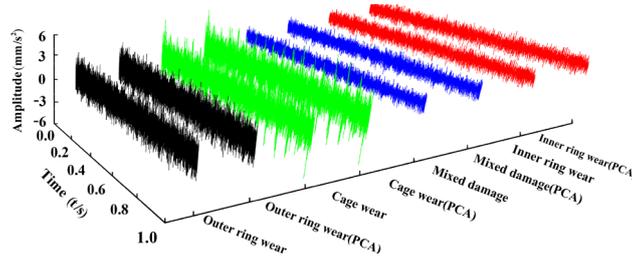


Fig.9 The different methods are used to screen the optimal reconstruction components of each fault: (a) Inner ring wear (EMD); (b) Inner ring wear (EEMD); (c) Inner ring wear (CEEMDAN); (d) Outer ring wear (EMD); (e) Outer ring wear (EEMD); (f) Outer ring wear (CEEMDAN); (g) Mixed damage (EMD); (h) Mixed damage (EEMD); (i) Mixed damage (CEEMDAN); (j) Cage wear (EMD); (k) Cage wear (EEMD); (l) Cage wear (CEEMDAN)

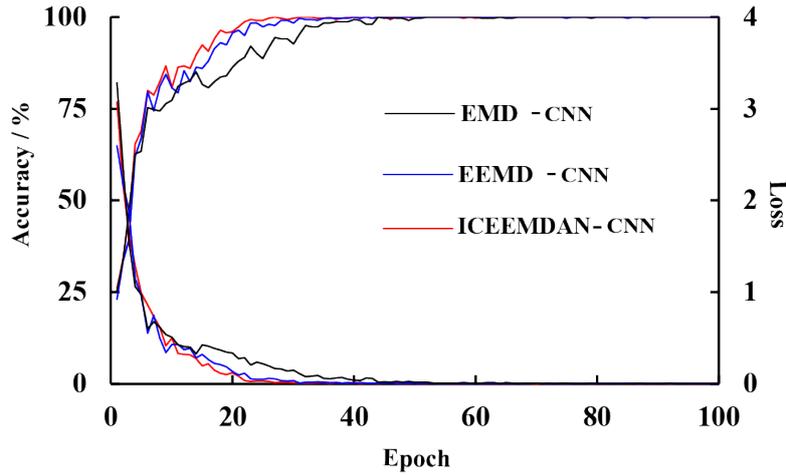
244 Fig.9 shows that fractal dimension is negatively correlated before and after PCA dimension reduction, and
 245 CEEMDAN algorithm is significantly superior to EMD and EEMD. Based on the properties of fractal box
 246 dimension, the size of box dimension can indirectly judge the stability of signal. Before using PCA to reduce
 247 dimension, the residual noise in IMF component directly affects the overall stability, which leads to the box
 248 dimension decreasing gradually with the component. After PCA dimensionality reduction, main fault information is
 249 further extracted and purified to enhance the stability of data. The cross method can not only avoid the influence of
 250 residual noise, but also eliminate redundant components and false components. The time domain diagram of the
 251 optimal reconstruction component group of each fault is shown in Fig.10.



252 Fig.10 The Time domain diagrams of the optimal reconstructed component group and the original signal component

253 4.3 Model performance verification

254 In order to better validate the proposed improved method and its performance, this paper compares
255 ICEEMDAN with EMD and EEMD algorithms: and inputs the optimized reconstructed filter component group into
256 CNN for fault diagnosis. In addition, The length of each segment of the original signal is 2048, and they have been
257 divided into training, testing, and validation sets in a ratio of 8:1:1. The training process consists of 10 epochs, with
258 10 iterations per epoch. The accuracy and loss of the validation set of the best reconstructed component in the
259 absence of noise are shown in Fig.11.

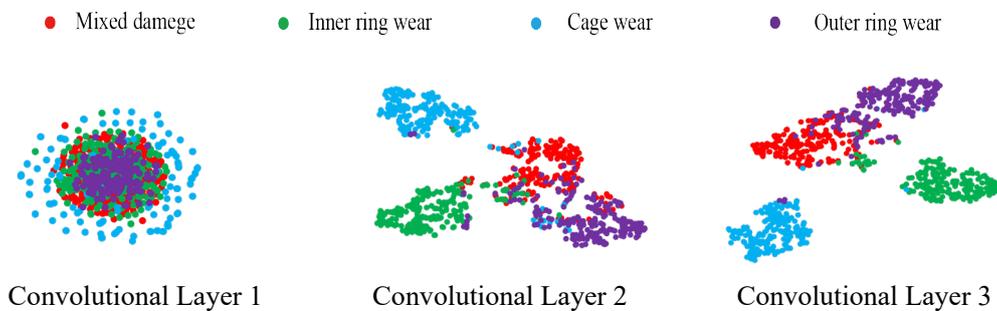


260 Fig.11 The accuracy and loss of validation for optimal reconstruction component

261 As can be seen from Fig.11, the ICEEMDAN-CNN method proposed in this paper is superior to other
262 algorithms in both accuracy and loss. However, there are mixed noises in the actual environment. In order to further
263 verify the practicability and generalization of the method, it is necessary to add noises with different SNR to the
264 signal to restore the actual operating environment as much as possible.

265 4.4 Visualization and Generalization comparison validation

266 Deep network learning is mostly based on the analysis of data attributes, which is difficult to restore the actual
267 complex operating conditions. Therefore, this paper not only adds noise-assisted comparison verification, but also
268 uses a comparison method to screen the optimal component groups with different entropy. It is compared with the
269 sample entropy and fuzzy entropy fault diagnosis methods which are widely used in many fields [68-69]. The
270 t-SNE clustering visualization analysis results under different SNR are shown in Fig.12.



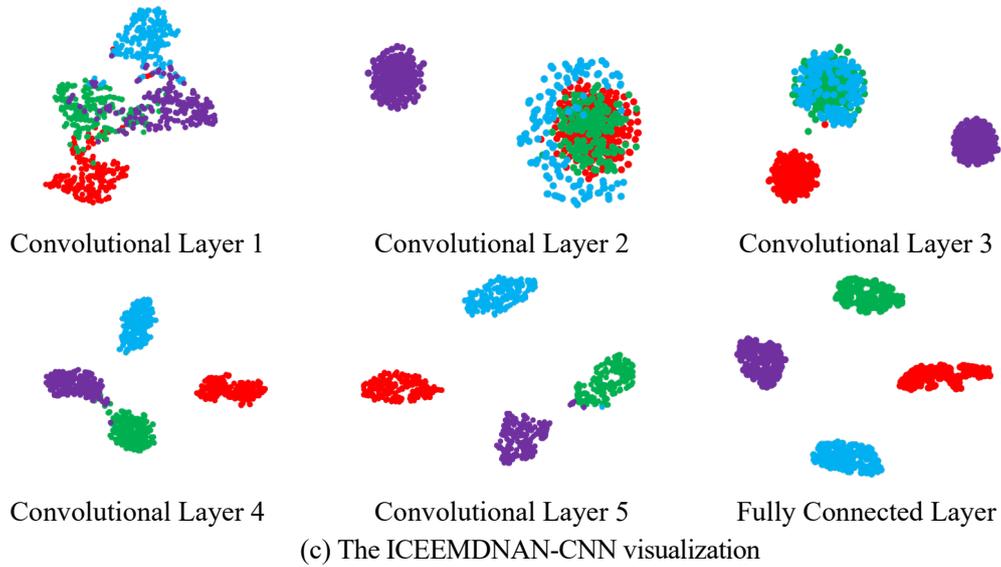
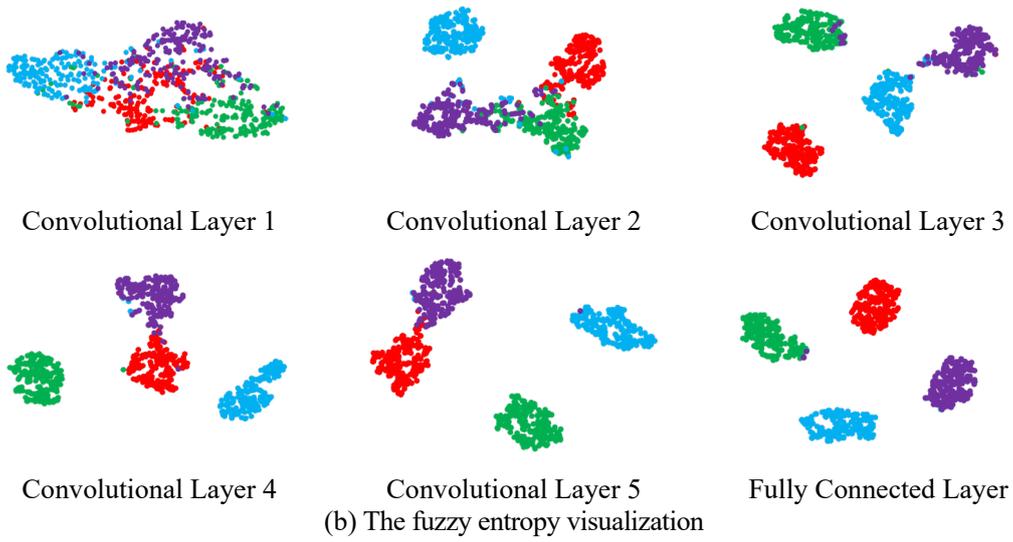
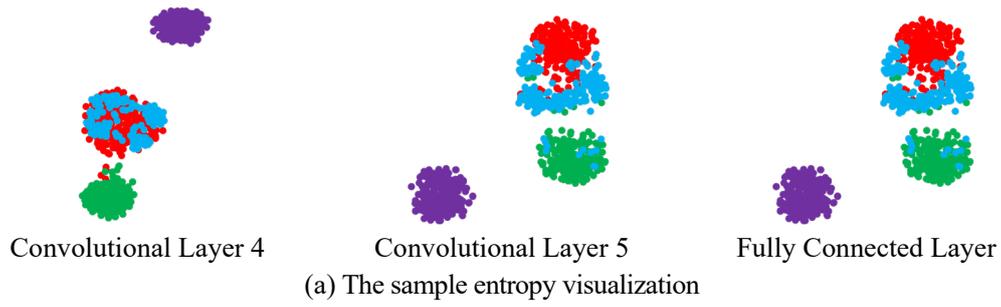


Fig.12 Visual analysis results of t-SNE clustering

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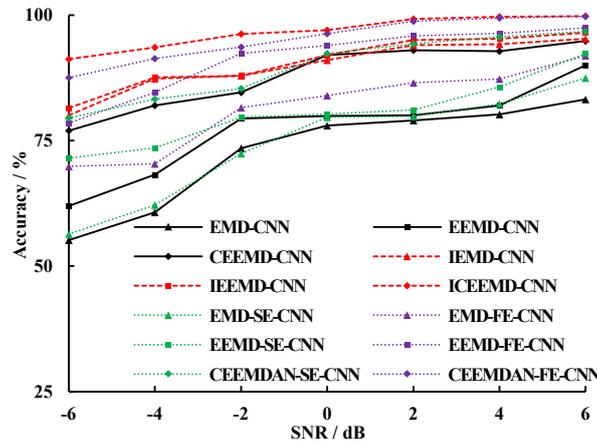
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278

279

Fig.12 shows that the data processed by deep network can be well classified by t-SNE clustering analysis method for the four kinds of rolling bearing faults. The proposed ICEEMDNAN-CNN method can completely separate the four faults, while the fuzzy entropy method is better than the sample entropy screening method, but they still cannot achieve the best clustering effect. The effect of noise on fault diagnosis can be better observed from the visualization results. It is evident that the choice of distinct methodologies for the selection and reconstruction of IMFs during the CEEMDAN procedure can exert a discernible influence on the ultimate performance of the entire model, The method substitutes PCA for sample entropy or fuzzy entropy to select and reconstruct IMF components during the CEEMDAN process. in this paper can better perform data mining for

280 massive high-dimensional big data, analyze the laws hidden behind the data, realizing fault classification and visual
 281 analysis. Therefore, the ICEEMDAN-CNN method proposed in this paper can better conduct data mining for
 282 massive and high-dimensional big data, exploring the laws hidden behind the data and realizing fault classification
 283 and visual analysis. In order to further highlight the good generalization performance of ICEEMDAN-CNN
 284 algorithm proposed in this paper, noises with different SNR were added to original signals and compared with
 285 existing methods respectively, and the results are shown in Fig.13.



286 Fig.13 The recognition accuracy of each method under different SNR

287 As shown in Fig.13, The proposed ICEEMDAN-CNN algorithm has obvious advantages and good
 288 generalization performance compared with other existing algorithms. The actual operating environment can be
 289 restored well under different SNR, and the correlation between SNR and accuracy is positive, which indirectly
 290 reflects the influence of noise on diagnosis accuracy. The improved algorithm has higher recognition and
 291 classification accuracy than the original algorithm. The accuracy of the proposed method is up to 99.79%, and the
 292 recognition accuracy is still 87.13% at the lowest SNR of -6dB, which is 0.54 - 10.33% higher than other
 293 algorithms. However, there is still room for improvement in this method at low (SNR)." In addition, it can eliminate
 294 redundant signals and false components well and realize noise reduction, enhance the accuracy of extracting
 295 effective fault signs, and further improve the accuracy of fault diagnosis recognition and classification.

296 5. Conclusions

297 A novel fault diagnosis method of rolling bearing is proposed using CNN and PCA fractal based feature
 298 extraction in this paper. The method can effectively solve the problems of redundant components and false
 299 components in the decomposition process of existing methods, screening also accurately the optimal component
 300 group. CEEMDAN algorithm is used to process raw signals to achieve noise reduction and decomposition. PCA
 301 can efficiently extract effective fault features by reducing the dimension of high-dimensional data, and fractal box
 302 dimension filters the best reconstruction component groups to eliminate irrelevant components. Finally, CNN
 303 further excavates the optimal component group to realize fault diagnosis recognition and classification. In addition,
 304 the effectiveness and feasibility of this method are verified by a variety of data verification and comparison with
 305 existing methods. The specific conclusions are as follows:

- 306 (i) The proposed model framework of ICEEMDAN-CNN fault diagnosis, testing by experiment, can
 307 effectively filter out the noise disturbance and accurately extract the effective fault features, achieving
 308 better classification effect of four kinds of rolling bearing faults and reducing the diagnosis error.
- 309 (ii) The PCA and fractal box dimension combine method are used to select the best reconstructed component
 310 groups, which can effectively eliminate redundant components and false components. The reconstructed

311 component group is input into CNN with strong nonlinear fitting ability, which can adaptively extract
312 features to eliminate the interference caused by human factors and improve the accuracy of CNN fault
313 identification and classification. The robustness and feasibility of the proposed method are verified by
314 rolling bearing fault analysis under different working conditions.

315 (iii) Compared with the existing fault diagnosis models, the proposed ICEEMDAN-CNN model has the
316 highest recognition accuracy by 99.79% at different SNR. Meanwhile, the generalization of the proposed
317 model method is superior to EMD-CNN, EEMD-CNN, CEEMDAN-CNN, CEEMDAN-SE-CNN,
318 CEEMDAN-FE-CNN, IEMD-CNN, IEEMD-CNN etc.

319 The following future the optimization model analyses are need to investigate multifractal and multiscale
320 convolutional neural networks. In addition, the effect of adding different forms of noise on generalization can also
321 be considered.

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