



## LJMU Research Online

**Tabrizian, A, Tatar, M, Masdari, M, Eivazi, H and Seddighi, M**

**An experimental study on boundary layer transition detection over a pitching supercritical airfoil using hot-film sensors**

<http://researchonline.ljmu.ac.uk/id/eprint/14028/>

### Article

**Citation** (please note it is advisable to refer to the publisher's version if you intend to cite from this work)

**Tabrizian, A, Tatar, M, Masdari, M, Eivazi, H and Seddighi, M (2020) An experimental study on boundary layer transition detection over a pitching supercritical airfoil using hot-film sensors. International Journal of Heat and Fluid Flow. 86. ISSN 0142-727X**

LJMU has developed **LJMU Research Online** for users to access the research output of the University more effectively. Copyright © and Moral Rights for the papers on this site are retained by the individual authors and/or other copyright owners. Users may download and/or print one copy of any article(s) in LJMU Research Online to facilitate their private study or for non-commercial research. You may not engage in further distribution of the material or use it for any profit-making activities or any commercial gain.

The version presented here may differ from the published version or from the version of the record. Please see the repository URL above for details on accessing the published version and note that access may require a subscription.

For more information please contact [researchonline@ljmu.ac.uk](mailto:researchonline@ljmu.ac.uk)

<http://researchonline.ljmu.ac.uk/>

1 An Experimental Study on Boundary Layer Transition  
2 Detection Over a Pitching Supercritical Airfoil Using  
3 Hot-Film Sensors

4 Arshia Tabrizian<sup>a</sup>, Massoud Tatar<sup>a</sup>, Mehran Masdari<sup>a,\*</sup>, Hamidreza Eivazi<sup>a</sup>,  
5 Mehdi Seddighi<sup>b,\*</sup>

6 <sup>a</sup>*Faculty of New Sciences and Technologies, University of Tehran, Tehran, Iran*

7 <sup>b</sup>*Associate Prof., Department of Maritime and Mechanical Engineering, Liverpool John*  
8 *Moores University, Liverpool, United Kingdom*

---

9 **Abstract**

10 In the present work, experimental tests are conducted to study boundary  
11 layer transition over a supercritical airfoil undergoing pitch oscillations using  
12 hot-film sensors. Tests have been undertaken at an incompressible flow. Three  
13 reduced frequencies of oscillations and two mean angles of attack are studied and  
14 the influences of those parameters on transition location are discussed. Different  
15 algorithms are examined on the hot-film signals to detect the transition point.  
16 Results show the formation of a laminar separation bubble near the leading  
17 edge and at relatively higher angles of attack which leads to the transition of  
18 the boundary layer. However, at lower angles of attack, the amplification of the  
19 peaks in voltage signal indicate the emergence of the vortical structures within  
20 the boundary layer, introducing a different transition mechanism. Moreover, an  
21 increase in reduced frequency leads to a delay in transition onset, postponing it  
22 to a higher angle of attack, which widens the hysteresis between the upstroke  
23 and downstroke motions. Rising the reduced frequency yields in weakening or  
24 omission of vortical disturbances ensuing the removal of spikes in the signals. Of  
25 the other important results observed, is faster movement of the relaminarization  
26 point in the higher mean angle of attack. Finally, a time-frequency analysis of  
27 the hot-film signals is performed to investigate evolution of spectral features of  
28 the transition due to the pitching motion. An asymmetry is clearly observed in  
29 frequency pattern of the signals far from the bubble zone towards the trailing

1 edge; this may reflect the difference between the transition and relaminarization  
 2 physics. Also, various ranges of frequency were obtained for different transition  
 3 mechanisms.  
 4 *Keywords:* Boundary layer transition, Pitching airfoil, Hot-film measurement,  
 5 Time-frequency analysis, Laminar separation bubble

---

6

<b>Nomenclature</b>	$a$	Wavelet transform frequency scale	
<b>Abbreviations</b>	$b$	Wavelet transform time scale	
$\alpha$ , AOA	Angle of attack	$C$	Wavelet coefficient
CTA	Constant temperature anemometer	$c$	Chord length
LSB	Laminar separation bubble	$C^*$	Wavelet coefficient complex conjugate
PIV	Particle image velocimetry	$f$	Pitching motion frequency
$Re$	Reynolds number( $\frac{cU_\infty}{\nu}$ )	$f_0$	Central frequency of wavelet function
<b>Symbols</b>			
$\alpha_0$	Mean angle of attack	$k$	Reduced frequency ( $\frac{\pi fc}{U_\infty}$ )
$\alpha_{amp.}$	Pitching amplitude	$S$	Skewness
$\omega$	Angular velocity in pitching motion	$s$	Curved distance from LE
$\sigma$	Standard deviation	$T$	Cycle period
$\varphi$	Wavelet function	$U$	CTA Output voltage
$\varphi^*$	Wavelet function complex conjugate	$x$	Distance from LE along the chord

## 7 1. Introduction

8 Drag reduction is one of the preliminary considerations in state-of-the-art  
 9 aerodynamic designs. For the purpose of skin friction reduction, it is of interest  
 10 to keep a significant portion of the boundary layer over a wing in the laminar  
 11 state. However, the transition from laminar to turbulence leads to an increase  
 12 in the total shear stress and the heat exchanged between the wall surface and  
 13 the flow. Depending on the turbulence level of the freestream flow, the pressure

1 gradient along the laminar boundary layer, the geometrical details, and the sur-  
2 face roughness, there are various possible mechanisms that may take the flow  
3 to the transition, e.g. natural, bypass, separated flow, periodic-unsteady, and  
4 reverse transitions. In natural transition, where the level of freestream turbu-  
5 lence intensity is less than 1%, transition is typically the result of disturbances  
6 growth in the flow, such as Tollmein-Schlichting (T-S) waves or cross-flow in-  
7 stabilities. These two-dimensional waves are amplified and three-dimensional  
8 hair-pin vortices are formed. Finally, areas of turbulence, denoted as turbulent  
9 spots, start to develop in the streamwise direction. In bypass transition where  
10 the level of turbulence in the free-stream is high, the transition is usually seen  
11 at a significantly lower Reynolds number, and the mechanisms by which the  
12 transition occurs often involve no or little T-S waves. In these two transition  
13 mechanisms, vortical patterns within the transition region are called “coherent  
14 structures” which are responsible for skin friction drag and heat transfer in-  
15 crease. Another important category is the separation-induced transition, first  
16 introduced by Mayle [1]. In this mechanism, the laminar boundary layer sepa-  
17 rates under the influence of a pressure gradient and transition develops within  
18 the separated shear layer as a result of an inviscid instability mechanism. At  
19 the point that the flow reattaches, a laminar-separation/turbulent-reattachment  
20 bubble is formed on the surface.

21 Although there are considerable improvements in transition detection in  
22 steady flows and over the rigid structures, the effect of unsteadiness of the  
23 rotating or oscillating blades and surfaces on the boundary layer state is still  
24 ascertainable. Boundary layer transition location is a significant aerodynamic  
25 characteristic to be examined in design of modern rotorcrafts and wind turbines.  
26 The main flow features in such applications are associated with the principals of  
27 the flow over the pitching airfoils. Due to the complexity of the transition detec-  
28 tion on oscillating airfoils and due to the lack of certain knowledge of unsteady  
29 transition, numerous designs have still relied on the steady transition charac-  
30 teristics. However, with the development of transition detection techniques and  
31 signal processing methods, modern designs can benefit taking the effects of un-

1 steady transition into account. Early transition-detection methods were based  
2 on visual detection of the transition location using a variety of methods such as  
3 smoke wire technique and surface oil method [2, 3]. Currently, most pervasive  
4 measurement techniques for transition detection rely on the measurement of sur-  
5 face shear stress and temperature variation, which are prompted by the change  
6 in boundary layer state. For instance, measurements of shear stress fluctuations  
7 were conducted across laminar, transitional, and turbulent boundary layers on  
8 a flat plate employing hot-film probes by Owen [4]. Armistead and Keyes [5]  
9 studied local turbulence-induced fluctuations in the pipe flow of water for a  
10 Reynolds number range of  $1.1 \times 10^4$  to  $1.7 \times 10^5$  using flush-mounted hot-film  
11 sensors. Moen and Schneider [6] studied a shock-induced boundary layer with  
12 the aim of determination of the effect of sensor size on the performance of flush-  
13 mounted hot-film sensors. Schulte and Hodson [7] employed surface-mounted  
14 hot-film gauges for investigation in the development of the unsteady suction side  
15 boundary layer of a highly loaded low pressure turbine blade. Lee and Wu [8]  
16 presented a comparison of experimental results on transition of wall-bounded  
17 flows obtained by hot-film measurement, flow visualisations, and particle image  
18 velocimetry (PIV).

19 In addition, infrared thermography technique has been successfully imple-  
20 mented for transition detection. Horstmann et al. [9] introduced the transition  
21 location as the position where the wall shear stress is increased on a special  
22 wing glove using infrared image technique. Gartenberg et al. [10] developed  
23 an experimental method based on infrared imaging for transition detection in  
24 cryogenic wind tunnels. However, due to the presence of high frequency phe-  
25 nomena in transition of the pitching airfoils, the higher time resolution tools  
26 are absolutely preferred for transition detection. Hot-film anemometry is the  
27 most successful and applicable technique for capturing the unsteady transition  
28 region while other methods are applied as well. Pascazio et al. [11] employed  
29 embedded laser velocimetry measurement method for unsteady boundary layer  
30 measurements on a NACA0012 oscillating airfoil. Kim and Chang [12] stud-  
31 ied the effect of low Reynolds number on the aerodynamic characteristics of a

1 pitching NACA0012 airfoil. Their results indicated that an increase in Reynolds  
2 number promotes the occurrence of boundary layer events such as laminar separa-  
3 tion and transition. Nati et al. [13] investigated the effect of a pitching motion  
4 on the characteristics of an LSB over the SD7003 airfoil using time-resolved pla-  
5 nar and tomographic PIV where separation, transition, and vortex roll-up onset  
6 were studied. The unsteady flow on a pitching LS(1) 0417 airfoil was experimen-  
7 tally investigated using micro-electro-mechanical systems thermal flow sensors  
8 by Leu et al. [14] benefiting from high spatial resolutions and response times as  
9 well as minimal interference of these sensors with the flow.

10 Transitional boundary layer flows have been the subject of several research  
11 studies. Vlahostergios et al. [15] introduced a cubic non-linear eddy-viscosity  
12 model combined with the laminar kinetic energy to model the separation-induced  
13 transition on a flat plate with a semi-circular leading edge. Compared with the  
14 linear model, it was reported that the proposed combined model behaves better  
15 in cases where the freestream turbulence intensity is low. Suluksna et al. [16]  
16 proposed mathematical expressions for two significant parameters to control the  
17 onset location and length of transition in the  $\gamma - Re_\theta$  four-equation transition  
18 model. They concluded that the correlation for the Reynolds number based  
19 on momentum thickness needs only to be expressed in terms of local turbu-  
20 lence intensity, so that the more complex form of the correlation that includes  
21 pressure gradient effects is unnecessary. Bernardini et al. [17] investigated the  
22 effect of compressibility on roughness induced boundary layer transition up to  
23 Mach number 4 by considering variations in the roughness height using direct  
24 numerical simulations. They found an identical vortex organization for all flow  
25 cases that experience transition, regardless of the Mach number. It was the  
26 generation of streamwise and wall-normal vorticity with the formation of an  
27 unstable detached shear-layer on the top of the element. Serna and Lázaro [18]  
28 experimentally investigated the laminar separation bubble (LSB) using laser  
29 based flow diagnostics. Proper understanding of the boundary layer state and  
30 transition point location is required in the aerodynamic design of air vehicles,  
31 and it has been the main incentive for many researchers ([19–21]). Kubacki and

1 Dick [22] presented a simple algebraic model for laminar to turbulent transition  
2 in boundary layers subjected to elevated free-stream turbulence. The model  
3 was combined with the  $k-\omega$  RANS turbulence model by Wilcox. The transi-  
4 tion model included the effects of both filtering of high-frequency free-stream  
5 disturbances by shear and breakdown of near-wall disturbances into fine-scale  
6 turbulence. Qingqing Ye et al. [23] studied the boundary layer transition over  
7 isolated roughness elements in the incompressible flow regime using tomographic  
8 PIV. To compare the different flow topologies and study the effect of the element  
9 shape on accelerating boundary layer transition, four different geometries (cylin-  
10 der, square, hemisphere and micro-ramp) were considered maintaining constant  
11 height. Medina et al. [24] conducted a new model for predicting pretransitional  
12 boundary layer fluctuations using the laminar kinetic energy concept for repre-  
13 senting them into the OpenFOAM solver.

14 Unsteady boundary layer transition on oscillating airfoils has been charac-  
15 terised for a range of pitch rates and Reynolds numbers using hot-film anemome-  
16 try. Surface shear-stress measurements were conducted by Kiedaisch and Acharya  
17 [25] on pitching NACA0012 airfoil at a constant rate from 0 to 45° using ar-  
18 ray of hot-film sensors. Unsteady boundary layer reversal and transition on  
19 a NACA0015 airfoil were studied by Schreck et al. [26] for a range of pitch  
20 rates and Reynolds numbers with the aim of determination of the unsteady flow  
21 physics crucial for control of the dynamically separated flows. Lee and Basu  
22 [27] measured the unsteady boundary layer features over a pitching NACA0012  
23 airfoil within and beyond the static-stall angle. They indicated that the pitch  
24 up motion assists to keep the boundary layer laminar at a higher angle of attack  
25 in comparison to that could be attained in static condition. Transition processes  
26 in the boundary layer of a high-pressure turbine rotor blade were investigated by  
27 Tiedemann and Kost [28]. The results were based on time-resolved, qualitative  
28 wall shear stress data, which was derived from surface hot-film measurements.  
29 Lee and Gerontakos [29] investigated the characteristics of the unsteady bound-  
30 ary layer and stall features on an oscillating NACA0012 airfoil using closely  
31 spaced multiple hot-film sensor arrays at  $Re = 1.35 \times 10^5$  with particular at-

1 attention to the spatial-temporal progression of the location of the transition and  
2 separation. Yarusevych et al. [30] conducted a series of experiment on transition  
3 of NACA 0025 airfoil. They observed that laminarly separated shear layer fails  
4 to attach to the surface in lower Reynolds number, but it leads to reattachment  
5 in higher one. Since the experimental results and the linear stability theory were  
6 in a good agreement, they figured out that the formation of the roll-up vortices  
7 can be essentially considered inviscid in nature. Masdari et al. [31] carried out  
8 an experimental investigation on a supercritical airfoil, calculating the bound-  
9 ary layer velocity profile and its dominant frequencies. They found that there  
10 is a frequency mode at which the oscillation frequency of the airfoil is the dom-  
11 inant frequency and functions as a factor causing turbulence in relation with  
12 the amplitude of oscillation of the airfoil. Also, Tabrizian et al. [32] performed  
13 a discrete wavelet transform on collected data from a boundary layer velocity  
14 profile of a supercritical airfoil in a pitch-hold-return motion. They resolved  
15 a vortex formation frequency inside boundary layer during upstroke motion.  
16 Rudmin et al. [33] presented a method for laminar separation and transition  
17 detection over a slowly pitching airfoil, with a frequency of 0.025 Hz, based on  
18 hot-film sensors responses. The proposed method was based on the windowed  
19 correlation between adjacent hot-film signals and the observation of the signal  
20 spectra but only applied on the static and the quasi-static cases. The same  
21 detection method was applied on a pitching airfoil to study the boundary layer  
22 behavior, and results were compared against the results obtained from Large  
23 Eddy Simulation (LES) [34]. Tatar et al. [35] investigated the effects of reduced  
24 frequency on the transitional boundary layer over a NACA0012 pitching airfoil  
25 using intermittency-based  $k - \omega$  shear stress transport model. They reported  
26 a delay in the chordwise boundary layer transition point by increasing the re-  
27 duced frequency and a vortex shedding within the LSB. Gardner and Richter  
28 [36] presented a method based on the analysis of the standard deviation of the  
29 surface pressure distribution for unsteady transition detection. The peak in  
30 the standard deviation of the pressure distribution is used as a measure of the  
31 transition position. The method was further developed to an analysis algorithm



1 utilizing the skewness for the detection of the transition on the pitching airfoil  
2 DSA-9A from the hot-film data [37].

3 As noted above, extensive studies have been conducted on detecting bound-  
4 ary layer transition over the moving airfoils. However, most of the studies  
5 focused on the "common" geometries such as NACA series airfoils. In the  
6 present work, efforts were made to study boundary layer transition onset over  
7 a pitching supercritical airfoil at off-design flow condition. Supercritical airfoils  
8 were designed to reduce drag at high transonic regime by means of a mostly-  
9 flat upper surface and a big curvature is also considered at the lower surface  
10 near the trailing edge to compensate the lift loss caused by flat upper surface.  
11 This causes an unknown behavior of this type of airfoils at incompressible flow  
12 regime and Reynolds number lower than that of the design point. Hot-film  
13 measurements over the upper surface of a supercritical airfoil which undergoes  
14 sinusoidal pitching motions at  $Re = 8.11 \times 10^5$ , are presented and the effects  
15 of reduced frequency and mean angle of attack are studied. More interestingly,  
16 versatile methods for transition detection are examined along with an automatic  
17 algorithm for peak capturing in order to prevent bias on transition detection.  
18 Moreover, time-frequency analysis is performed to find out the frequency con-  
19 tent and evolution of the transition mechanism. A proper wavelet method is  
20 employed to investigate the emerged frequencies during the transition in spatial-  
21 temporal domain. The analysis enables one to achieve a range of existing and  
22 emerging frequencies in transition process over a cycle of oscillation. Using  
23 wavelet method to capture dominant frequencies in shear layer and during the  
24 transition is a novel method that will be discussed further in this study.

## 25 **2. Experimental apparatus**

26 The tests were conducted in an open test section Gottingen-type wind tunnel  
27 with the maximum turbulence intensity of 0.4% at 35 m/s and at where the  
28 model was located. To reduce the open test section jet effects and to assure  
29 that the flow uniformity is within an acceptable range, a temporary wooden test

1 section (2.5 m  $\times$  1 m) is placed just after the contraction outlet. A stainless  
 2 steel straight section of a supercritical airfoil (RAE5215) with the chord of 40  
 3 cm was selected to investigate the transition behavior over its upper surface.  
 4 The model had the maximum thickness of 9.8% and was installed vertically in  
 5 the test section along with two 1m-diameter end plates in order to guarantee the  
 6 two-dimensional flow condition, occupying about 2.5% of temporary test section  
 7 frontal area while stayed at 8° AOA. Also, to ensure the 2D flow over the airfoil,  
 8 the mean flow uniformity has been examined over 30% of airfoil's span from mid  
 9 section containing the region where the hot-film arrays were installed. For the  
 10 test condition, the Reynolds number was obtained about  $8.11 \times 10^5$  based on  
 11 the free stream velocity and the airfoil chord. Figure 1 shows the airfoil section.

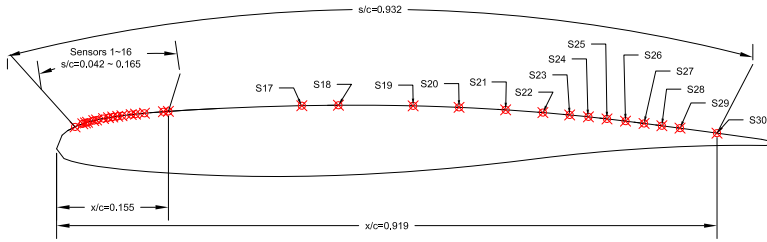


Figure 1: The airfoil section and the hot-film sensors location.

12 The upper surface was covered with two sheets of Senflex™ hot-film arrays  
 13 having 64 and 100 sensor elements with the normal elements spacing of 0.1  
 14 inches. However, the 64-element sheet had half sensor spacing at the middle  
 15 and was attached to the forward section of upper surface where the transition  
 16 region was expected to be emerged. Also, the 100-element sheet was adhered  
 17 just behind the first sheet in a manner that ensured all the sensors were in the  
 18 same direction over the upper surface (Fig. 2). Moreover, there were restrictions  
 19 on the quantity of hot-film sensors and more spacing was considered between the  
 20 sensors on the upper surface at some points. Nevertheless, it is worth nothing  
 21 that the sensors' arrangement has provided the ability of transition detection  
 22 and more future investigations.

23 A 30-channel constant temperature anemometer complete with a 16-bit em-

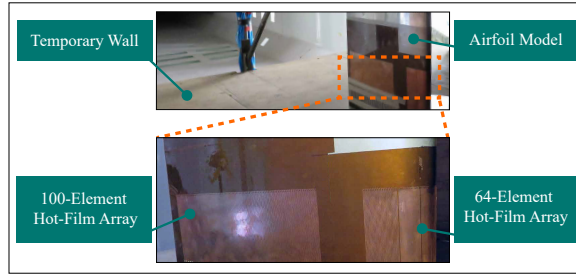


Figure 2: Airfoil model with hot-film sensors in the open test section.

1 bedded data acquisition system was employed to commission the hot-film sensors  
 2 and the output voltages were collected at the rate of 2.4 kHz. Also, the set-up  
 3 was equipped with an output trigger of 3.3 V, transmitted immediately after  
 4 the start of data acquisition. This trigger signal was important to synchronize  
 5 the hot-film outputs with the instantaneous angle of attack. The connection  
 6 diagram and the sequence of the events are shown in Fig. 3.

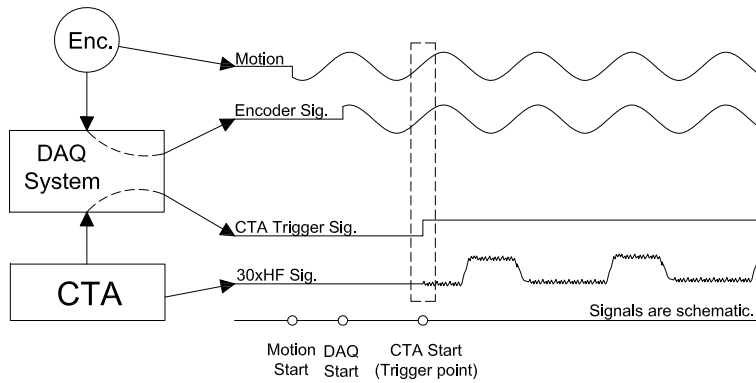


Figure 3: Data acquisition configuration and timeline.

7 A 750 W servo motor along with a proper drive were used to generate the  
 8 pure pitching motion via a four-bar linkage mechanism, capable of producing  
 9 pitching oscillation with the maximum frequency of 5 Hz. Figure 4 depicts a  
 10 schematic of the pitching oscillation mechanism and the equation of motion  
 11 is as Eq. (1). The value of instantaneous angle of attack was measured by a  
 12 12-bit differential rotary shaft encoder, directly connected to the airfoil shaft

1 at quarter chord. Utilizing the CTA output trigger, the encoder output was  
 2 acquired concurrently with those of hot-films.

$$\alpha = \alpha_0 + \alpha_{\text{amp}} \sin(\omega t) \quad (1)$$

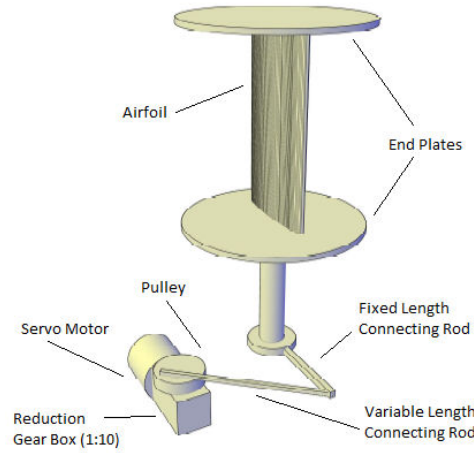


Figure 4: The pitching oscillation mechanism.

3 A process of uncertainty analysis was performed at the confidence level of  
 4 95% and the maximum uncertainty of output voltages was obtained 2.5%, comprising both bias and precision errors.

### 6 3. Results and discussion

7 Development of boundary layer is investigated on the upper surface of the  
 8 supercritical airfoil using hot-film sensors. The airfoil is oscillated sinusoidally  
 9 around its quarter-chord. Results are presented for three reduced frequencies  
 10 of 0.017, 0.035, and 0.053 and two mean angles of attack of  $0^\circ$  and  $4^\circ$ . For  
 11 all cases, the amplitude of pitching oscillation is selected equal to  $4^\circ$  at which  
 12 the transition was expected. Table 1 presents the test plan. Hereafter, the  
 13 cases with  $\alpha_0=0$  and  $\alpha_0=4^\circ$  may denote as case 1 and case 2, respectively. At  
 14 the beginning of this section, several transition and relaminarization detection

1 methods are verified. Also, the behaviour of the flow and corresponding events  
 2 are described. Then, the influence of reduced frequency and mean angle of  
 3 attack on the transition and relaminarization locations are studied. Eventually,  
 4 a temporal-spatial frequency analysis is employed, utilizing continuous wavelet  
 5 transform in order to provide a valuable insight to the existing phenomena over  
 6 the pitching airfoil.

Table 1: Test plan

Test case	$\alpha_0$ ( $^\circ$ )	$\alpha_{\text{amp}}$ ( $^\circ$ )	$k$
1	0	4	0.017, 0.035, 0.053
2	4	4	0.017, 0.035, 0.053

### 7 3.1. Transition point detection algorithms

8 Hot-film anemometry is one of the well-known techniques for unsteady bound-  
 9 ary layer transition detection. A traditional way of transition detection using  
 10 hot-film is to manually extract the detail of the transition from laminar to tur-  
 11 bulent flow from phase-averaged voltage signal of individual sensors and through  
 12 the visual interpretation of the changes in voltage levels. However, this manual  
 13 procedure demands both time and skill. Alternatively, a detection method was  
 14 developed allowing a computer-aided automated transition detection based on  
 15 the skewness of data. Skewness is a statistical characteristic and indicates the  
 16 level of asymmetry of the signal around its mean. The approach was earlier  
 17 implemented for determining the boundary layer state by Tiedemann [28]. In  
 18 addition to the skewness, other detection methods such as standard deviation  
 19 of the phase-averaged signal and the signal derivative have also been verified  
 20 here to assess the functionality of these methods in detection of the unsteady  
 21 boundary layer transition. The skewness, standard deviation, and derivative of  
 22 a hot-film signal at  $s/c = 0.165$  are shown in Fig. 5, respectively below the main  
 23 hot-film signal where the airfoil oscillates with the reduced frequency of 0.017,

1 and around the mean AOA of  $4^\circ$ . The time is normalized with the period of os-  
2 cillations ( $T$ ) to show the time of occurrence of boundary layer phenomena, e.g.,  
3 transition and relaminarization, in a cycle of airfoil oscillations. The skewness  
4 and standard deviation are evaluated utilizing a sliding window with the width  
5 of 5% of the period. It is worth noting that in Fig. 5 the results are presented  
6 in such a way that the minimum AOA occurs at  $t/T = 0$  and  $t/T = 1$ , and the  
7 maximum AOA is at  $t/T = 0.5$ . As depicted in Fig. 5, the flow is purely lam-  
8 inar at  $t/T \leq 0.21$  and  $t/T \geq 0.81$  and purely turbulent at  $0.31 \leq t/T \leq 0.72$ .  
9 Distribution of data in a single window is nearly normal, while at the start of  
10 transition, a sudden increase in the voltage signal leads to a deviation of the  
11 skewness from zero towards the positive values and a sudden rise in the standard  
12 deviation. A positive skewness in transition and near the laminar regions is due  
13 to the presence of a few number of disturbances with the high voltage values  
14 that cause the right tail of normal distribution to be longer. Near the turbulent  
15 region, however, the number of turbulent spots increases and the mode of data  
16 becomes greater than its mean, therefore the left tail is longer this time and  
17 the skewness returns negative values. At 50% intermittency, where the flow is  
18 literally in a balance between laminar and turbulent, the voltage distribution  
19 in a single window is almost symmetric. Hence, the skewness approaches zero  
20 again. Standard deviation, however, is rocketing. With the start of turbulent  
21 flow and fluctuation of the data in a window around its mean, the standard  
22 deviation decreases, and the skewness goes back to zero from negative values.  
23 It can be seen in Fig. 5 that the start and the end of laminar and turbulent  
24 flows are not accurately predicted from the skewness of the voltage signal where  
25 the standard deviation comparatively results in more reliable outcomes. The  
26 derivative of the signal using a central differencing approach obtains the most  
27 accurate points for the start and end of the fully laminar and turbulent flows.  
28 It should be noted that the selection of the window width is significant. With  
29 a low-width window, the skewness and standard deviation may manifest huge  
30 fluctuations, making it very difficult to extract desired (start and end) points  
31 from the obtained signals. Also, as it is seen in Fig. 5, the implementation of

1 a moderate width is more plausible for indicating the 50% intermittency point,  
2 since it better represents the existence of both laminar and turbulent flows at  
3 a specific period of time. Moreover, the peak of derivative does not make any  
4 physical sense to be a good criterion for 50% intermittency. Accordingly, in  
5 this study, the derivative of the voltage signal is used for extracting the start  
6 and the end of the laminar and turbulent flows, while the standard deviation is  
7 implemented for indicating the 50% intermittency.

### 8 *3.2. Transition and relaminarization phenomena over the upper surface*

9 The voltage signals of the sensors on the upper surface of the airfoil are  
10 demonstrated in Fig. 6 for the case 2 with the reduced frequency of 0.017. Also,  
11 the 50% intermittency locations during the transition and the relaminarization  
12 are marked on the figure. Near the leading edge, the presence of an LSB is  
13 notable at about  $0.31 < t/T < 0.68$ . A gradual increment of AOA causes an  
14 improvement of an adverse pressure gradient near the leading edge and the  
15 formation of the LSB. As a consequence of the laminar flow separation, the  
16 skin friction and hot-film heat transfer levels are reduced, and so, the level of  
17 voltage is declined. This region over the upper surface, marked as region 1 in  
18 the figure, experiences neither transition nor turbulent flow during the whole  
19 pitching cycle. However, with decrement of the AOA, the LSB vanishes and the  
20 the flow reattaches to the surface in a laminar state. Also, a little farther from  
21 the leading edge, at  $s/c = 0.087 \sim 0.165$  another voltage decay is detected which  
22 again represents formation of a separation bubble (at region 2) that usually  
23 emerges at the suction side of the airfoil caused by the same mechanism. In  
24 this case, the LSB lasts for a shorter time and is pursued by the transitional  
25 and turbulent regions evinced by a jump (region 3) to a higher levels of voltages  
26 with more fluctuations (region 4), respectively. The transition process starts  
27 with a sudden change in voltage right after the laminar state (region 7), but  
28 ends to turbulence with a slight voltage change. It is obvious that the LSB  
29 moves forward and stays more time on the airfoil surface as the AOA rises.  
30 It seems that its length is greater at higher angles, as well. After a period of

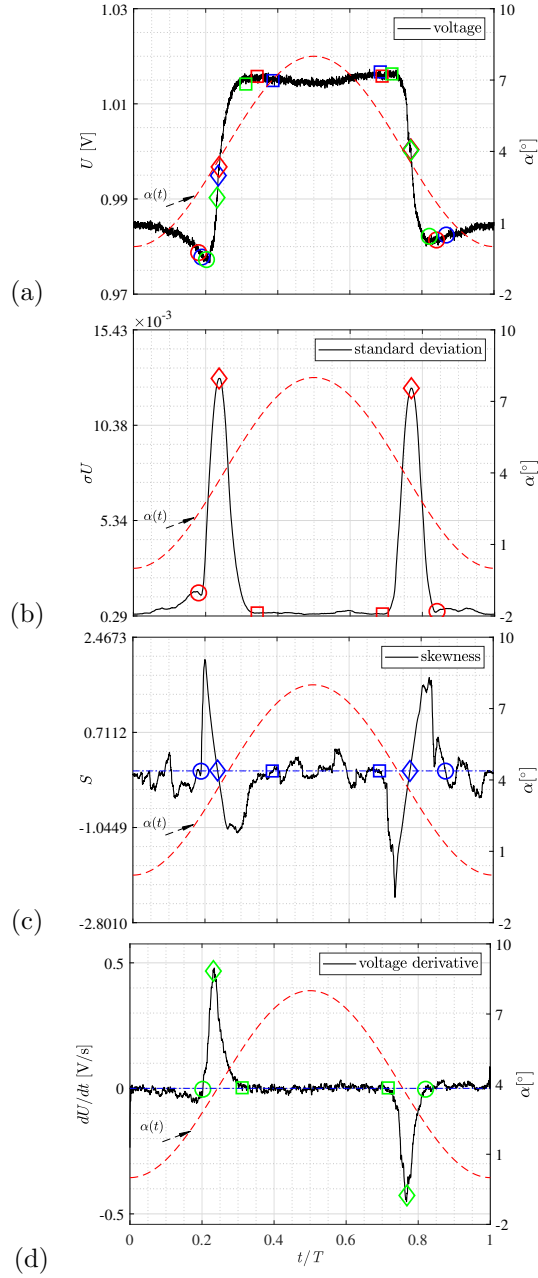


Figure 5: (a) Voltage signal, (b) skewness, (c) standard deviation, and (d) voltage derivative for the sensor at  $s/c = 0.165$  on the upper side; Case 2,  $k = 0.017$ . Start/end laminar flow: circle, 50% intermittency: diamond, start/end turbulent flow: square. Blue, red, and green markers indicate the points extracted from skewness, standard deviation, and voltage derivative, respectively.



1 turbulence on the surface, the relaminarization takes place in a reverse process of  
2 the transition. As the AOA decreases, the relaminarization (region 5) followed  
3 by a small separation region (region 6) and eventually laminar flow appears  
4 on the airfoil surface. The relaminarization process actually happens because  
5 of the presence of a favorable pressure gradient which completely collapses the  
6 turbulence. Moreover, a region of turbulent separation can also be observed  
7 on the sensor located at  $s/c = 0.932$  (region 9). As depicted in the figure, by  
8 increasing the AOA, the turbulent flow separates from the upper surface which  
9 is evinced by a slight reduction in the voltage of the signal.

10 Looking more accurate through the signal, for instance at  $t/T < 0.2$ , indi-  
11 cated by line (a), the flow is laminar on the upper surface for approximately  
12 35% of the chord. However, some spikes are emerged in the signal which are  
13 amplified with getting closer to the trailing edge. This process ends up in a  
14 turbulent region at  $s/c = 0.854$ . The gradual amplification of the perturbations  
15 may initially be attributed to the amplification of the T-S waves as the mech-  
16 anism for the natural transition to turbulent flow. At  $t/T < 0.3$ , designated  
17 by line (b), it is observed that the laminar flow passes over the upper surface  
18 and near the leading edge. At  $s/c = 0.081 \sim 0.132$ , the LSB is formed, and  
19 followed by a wide turbulent region up to  $s/c = 0.88$ . Then, a small separation  
20 of the turbulent boundary layer is perceived. At  $t/T = 0.5$ , traced by line (c),  
21 a separation bubble at the near-leading edge region is pursued by a turbulent  
22 flow at  $s/c = 0.081$  and further.

23 Also, near the trailing edge, at  $s/c = 0.777 \sim 0.88$ , a number of turbulent  
24 bursts is noticeable at low AOA below  $t/T = 0.11$  accompanying with a large  
25 portion of the fully turbulent flow in a period (region 8).

26 Apparently, two possible mechanisms of the boundary layer transition can  
27 be inferred from the behaviour of hot-film signals. Near the leading edge (lower  
28  $s/c$ ), a drop in the signal level flaunted just before its rise, introducing the  
29 occurrence of the LSB. However, moving towards the trailing edge at low  $t/T$   
30 where no LSB exists, a gradual amplification is observed for the signal level of the  
31 laminar to that of the turbulent regime. This reflects a transition mechanisms,

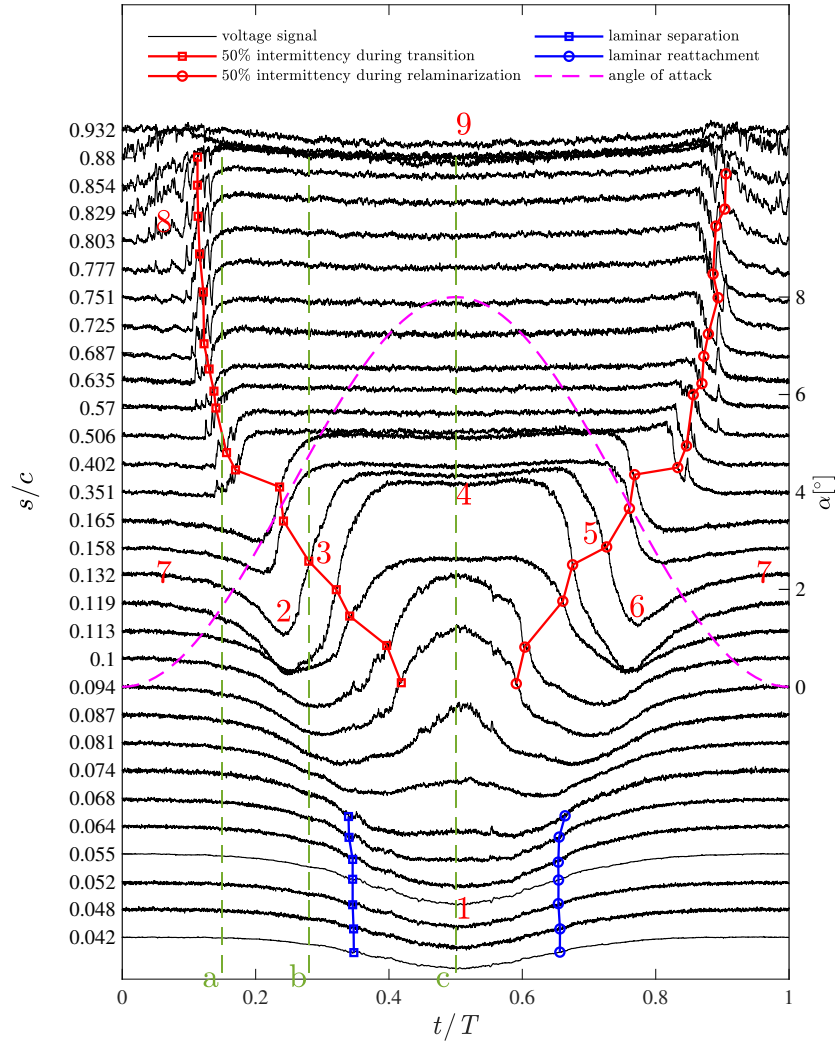


Figure 6: Voltage signal for all sensors on the upper surface of the airfoil; Case 2,  $k = 0.017$ . The vertical green dashed lines of a, b, and c represent  $t/T$  equal to 0.15, 0.28, and 0.5, respectively.

1 perhaps the natural one, which is completely different from the separation-  
2 induced transition process.

3 In Fig. 7, the movement of transition and relaminarization points on the  
4 upper surface is shown for the same previous case. As it was mentioned earlier,  
5 the start and the end of the transition region are identified using the derivative  
6 of the signal, and the 50% intermittency is marked as the peaks in the standard  
7 deviation of the signal. Whereas, by increasing the AOA the transition location  
8 is moved towards the leading edge, it is moved backward to the trailing edge  
9 while the AOA decreases. This generates a hysteresis between the upstroke and  
10 downstroke motions. In this case, the transition region moves on the upper  
11 surface between  $s/c = 0.087$  and  $s/c = 0.88$ ; however, at  $s/c = 0.88$ , the flow is  
12 uncertain between laminar and turbulent states at minimum AOA. Approaching  
13 to the trailing edge, no laminar flow is seen at  $s/c = 0.932$  and the boundary  
14 layer becomes fully turbulent. The rate of the transition region movement is  
15 fast during the first quarter of the oscillation cycle as the 50% intermittency  
16 point moves from  $s/c = 0.88$  at  $t/T = 0.043$  to  $s/c = 0.165$  at  $t/T = 0.235$ .  
17 Thereafter, it reduces during the second quarter of the cycle. In other words,  
18 there is a sudden change in the transition location before the  $2^\circ$  AOA which  
19 can be ensued from the flatness of the upper surface. Furthermore, the fraction  
20 of time of motion in which the boundary layer is fully turbulent is larger near  
21 the trailing edge positions compared to the ones at the leading edge.

### 22 *3.3. Influence of the reduced frequency*

23 The influence of the reduced frequency on the unsteady transition region is  
24 described in this section. First of all, as the airfoil chord and the freestream  
25 velocity were constant during the tests, the only effective parameter on reduced  
26 frequency is the pitching motion frequency. The airfoil oscillates with three  
27 reduced frequencies of 0.017, 0.035, and 0.053 and the results are presented for  
28 different oscillations. Locations of the 50% intermittency are shown over the  
29 upper surface of the airfoil and the extent of the turbulent region and the time  
30 delay between the transition movement and the airfoil motion are exhibited.

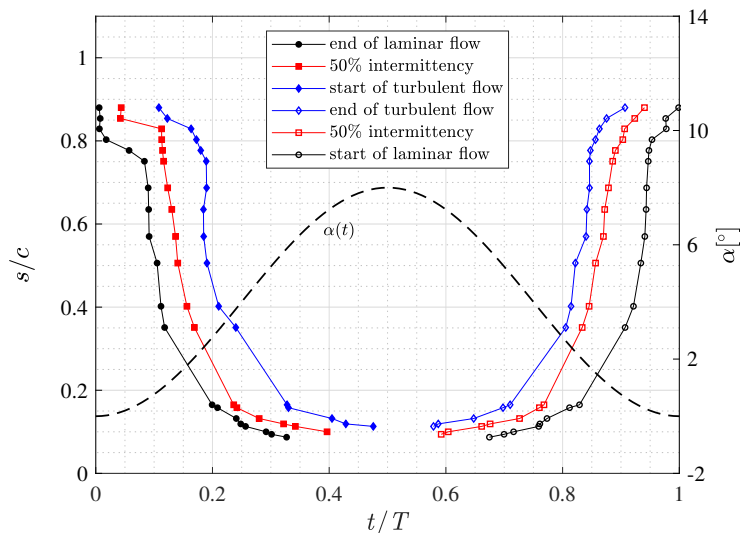


Figure 7: Variation of transition locations vs. the time; Case 2 for  $k = 0.017$ .

1 The transition locations against the non-dimensional time and the AOA, are  
2 depicted in Fig. 8 ~ Fig. 9 for oscillations of the case 1 and 2, respectively. As  
3 figures reveal, variation of the reduced frequency strongly affects the transition  
4 characteristics. An increase in  $k$  leads to a delay in the transition onset, post-  
5 posing it to a higher AOA; this results in a wider hysteresis between the upstroke  
6 and downstroke motions. The delay can be related to the apparent mass and  
7 unsteady features in the boundary layer which is more tangible as the  $k$  rises.  
8 For the sensor located at  $s/c = 0.635$  in case 2, this time lag is about  $0.07 t/T$   
9 between the oscillations with reduced frequencies of 0.017 and 0.035. For the  
10 oscillation with  $k = 0.017$ , transition and relaminarization happen nearly at the  
11 same angle of attack. Also, the pattern of the transition and relaminarization  
12 are almost symmetric with respect to the AOA. The more the  $k$  increases, the  
13 more the asymmetry appears in the pattern. As the lowest  $k$  is presumed to be  
14 in quasi-steady regime, the up/down strokes are roughly identical and are in a  
15 good agreement with the static result. However, as the reduced frequency rises,  
16 the corresponding apparent mass causes a wider hysteresis loop. Moreover, the  
17 trend of the transition movements are very similar for all frequencies in spite of

1 the range of reduced frequencies. Additionally, for the negative angles of attack  
2 the transition region is placed near the trailing edge and mild variation in its  
3 location is observed.

4 Case 2 has less agreement with the static condition in comparison to first  
5 case. This might be as a result of the fact that at higher AOA (greater than 2  
6 degrees) the location of 50% intermittency points are so close together and to  
7 the leading edge. Meanwhile, the airfoil motion makes a noticeable change in  
8 transition location as well. In addition, at higher reduced frequencies, a very  
9 rapid change in the location of the transition and relaminarization points is  
10 detected which can be called a rapid transition/relaminarization jump.

11 Figure 10 demonstrates time history of the hot-film signals for the oscil-  
12 lation case 2 and three reduced frequencies at  $s/c = 0.75$ . Some spikes are  
13 revealed by the signals which reflect formation of a vortex-like disturbance or  
14 a circulation region. As a result, a surge in the level of heat transfer is ex-  
15 pected. They emerge at a moment and vanish a moment later, therefore they  
16 appear as spikes. However, by increasing the reduced frequency, the signal's  
17 spikes diminish. Alternatively stated, a rise in the frequency of the pitching  
18 motion yields weakening or omission of such disturbances. As  $k$  increases, the  
19 existence of time lag which is an important inherent subject in unsteady flows is  
20 revealed. The trend of hot-film signal is slightly shifted to the right (higher in-  
21 stants), compared to variation of the angle of attack, reflecting a lag in hot-film  
22 response as to the motion. Hence, the flow faces to an angle of attack smaller  
23 than the actual one. Despite the lower  $k$  that the level of hot-film output de-  
24 clines at higher AOAs, implying the turbulent separation, no decrease is seen  
25 for the higher  $k$ . It is worth nothing that the same observations are found for  
26 the relaminarization process.

### 27 *3.4. Influence of mean angle of attack*

28 Figure 11 demonstrates the transition and relaminarization points against  
29 the AOA for the oscillating airfoil with mean AOAs of zero and 4 degrees,  
30 at three reduced frequencies. For the higher mean AOA, the flow experiences

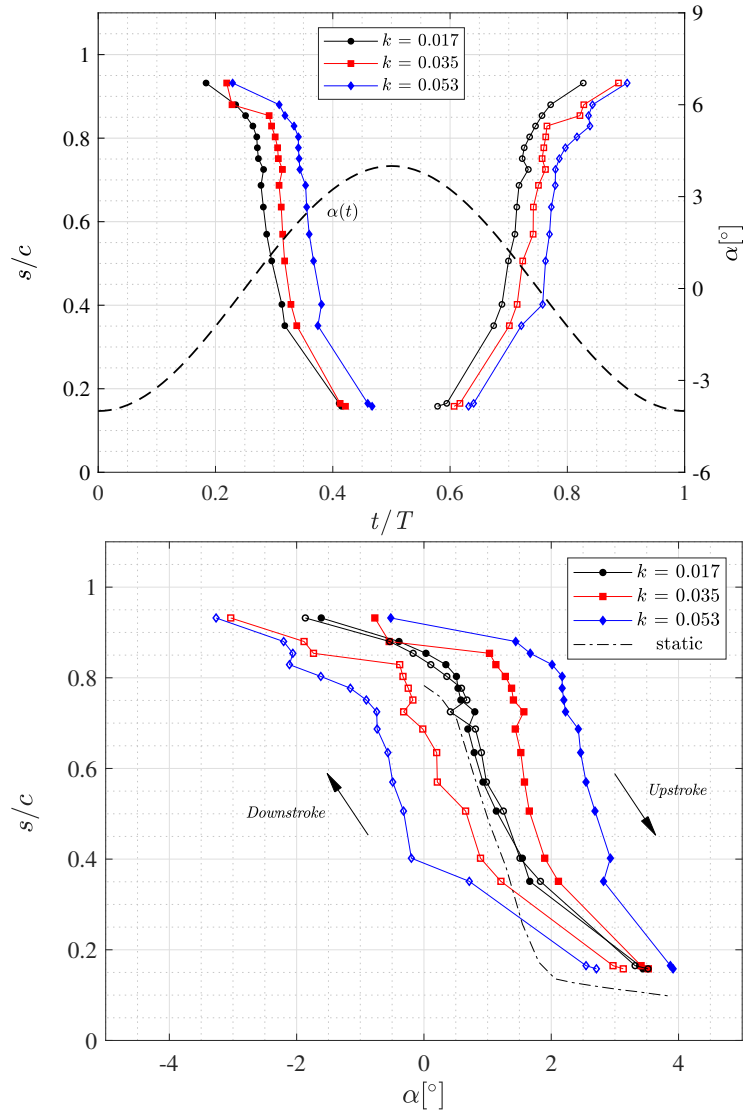


Figure 8: Variation of transition locations versus time (top) and angle of attack (bottom) for oscillation with various frequencies; Case 1.

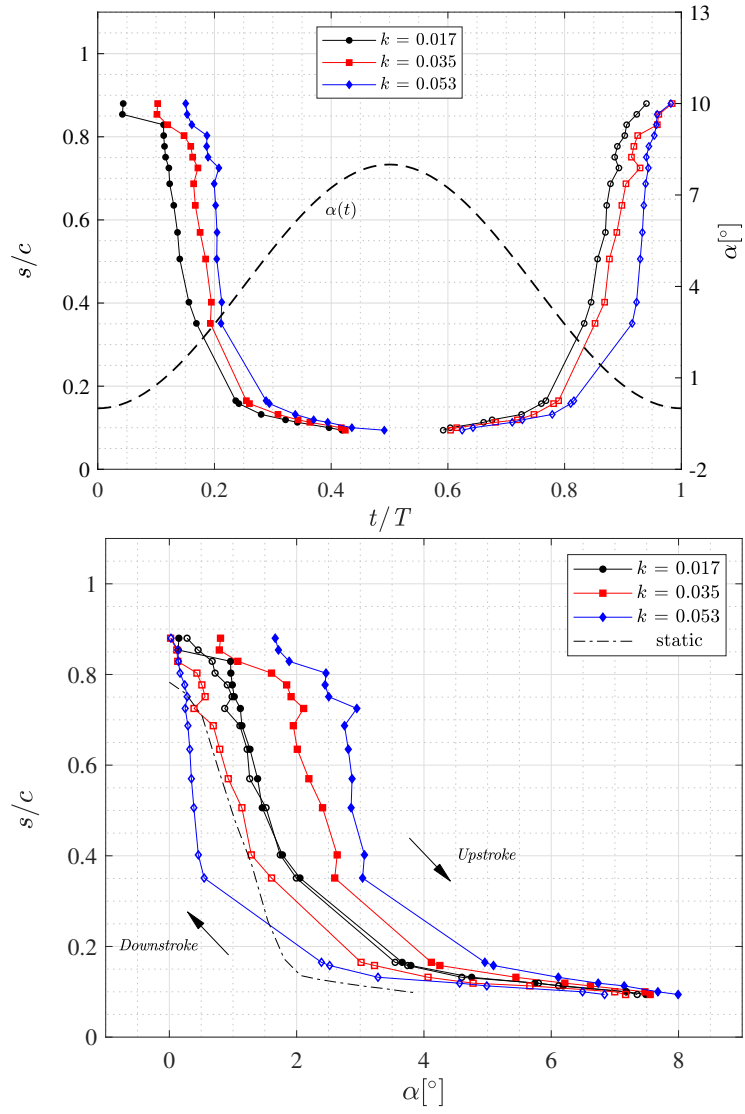


Figure 9: Variation of transition locations versus time (top) and angle of attack (bottom) for oscillation with various frequencies; Case 2.

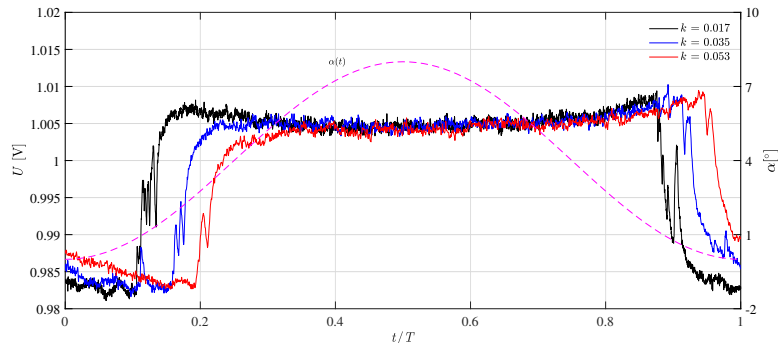


Figure 10: Hot-film signals at three reduced frequencies at  $s/c = 0.75$ , Case 2

1 turbulence over a more portion of a cycle which was expected due to higher  
 2 AOAs through which it passes. Moreover, at the  $k=0.017$ , variation of the  
 3 transition onset is broadly similar for both cases. Nevertheless, transition occurs  
 4 slightly in higher AOAs for  $\alpha_0 = 4^\circ$ . Although for the lower  $k$  which is quasi-  
 5 steady, no significant change in pattern of the transition and relaminarization  
 6 is detected, for the higher reduced frequencies transition and relaminarization  
 7 points move slightly faster in the case 2. On the other hand, for the higher  $k$ ,  
 8 the transition process is almost similar for both mean angles of attack, while the  
 9 relaminarization begins faster for case 2. Indeed, the relaminarization point for  
 10 AOAs less than  $1^\circ$ , dramatically moves towards the trailing edge in case 2, for  
 11 instance, at zero AOA, the relaminarization point for case 1 is about  $s/c = 0.4$ ,  
 12 while for case 2, it is close to the trailing edge. Conversely, as depicted in Fig. 11,  
 13 the location of relaminarization for negative AOAs gradually moves towards the  
 14 trailing edge. The location of this slope-change appears with a lag for higher  
 15 frequencies, though.

### 16 3.5. Time-Frequency Analysis

Wavelets, introduced by Grossmann and Morlet [38], have been extensively adopted in many areas of science and engineering. In fluid mechanics, wavelets were first used in the early 1990s to analyze turbulent flows ([39] and [40]). Continuous wavelet analysis can be used to study how spectral features evolve over time, identify common time-varying patterns in signals, and perform time-



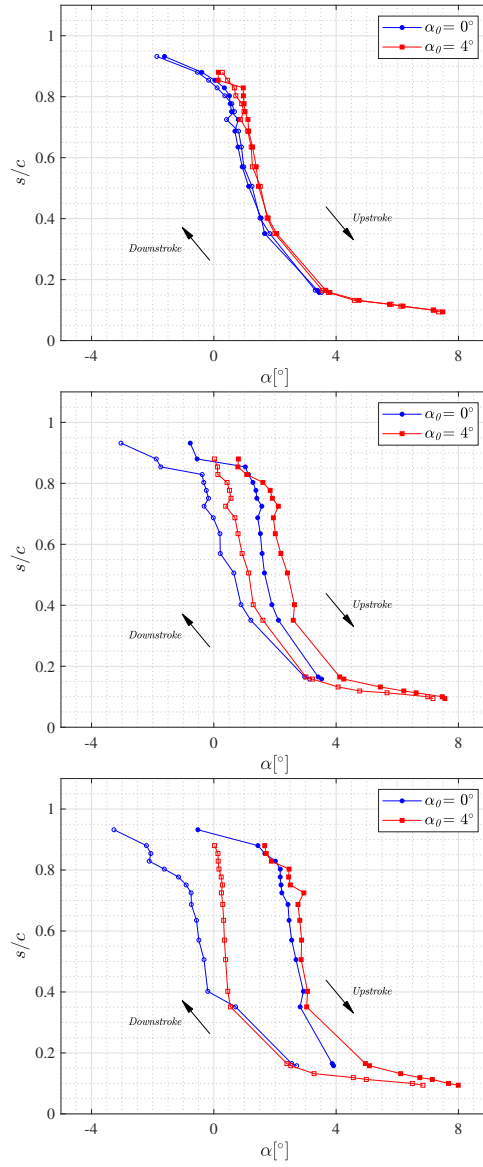


Figure 11: Variation of transition locations versus  $\alpha$  for oscillations with two mean angles of attack and three reduced frequencies;  $k = 0.017$  (top),  $k = 0.035$  (middle),  $k = 0.053$  (bottom).

localized filtering. In the present study, the complex Morlet wavelet ([38]) is used to analyze hot-film signal at each sensor position. The wavelet transform is given as:

$$\varphi(t) = \frac{1}{\sqrt{4\pi}} e^{2i\pi f_0 t} e^{-t^2/2} \quad (2)$$

1 and the wavelet transform coefficients are defined as:

$$C(a, b) = \frac{1}{\sqrt{a}} \int_{-\infty}^{+\infty} U(t) \varphi^* \left( \frac{t-b}{a} \right) dt \quad (3)$$

2 Figure 12 shows the absolute value of the wavelet transform coefficients for 8  
3 locations over the upper surface during a period of motion for case 2 at  $k =$   
4 0.017. Also included in the plots, are the hot-film sensors output.

5 Regarding Fig. 12, at  $s/c = 0.048$ , the level of signal first decreases due  
6 to the presence of the leading edge laminar separation bubble where the local  
7 velocity of the flow and hence the wall shear stress lessen. The corresponding  
8 wavelet content shows a very low frequency, almost steady, low intensity spots  
9 representing the bubble region. At  $s/c = 0.068$ , the same events are exhibited.  
10 Compared with the previous position, the level of signal as well as frequency  
11 components are grown. This phenomenon can denote the initiation of the flow  
12 fluctuations within the concept of “laminar-kinetic-energy” which was proposed  
13 by Mayle and Schulz [41]. A clear strengthen of low frequencies, within the  
14 range of 10-15 Hz., is seen for this location. Moving toward the trailing edge on  
15 the upper surface, it appears that the boundary layer transition first occurs at  
16  $s/c = 0.094$ . The separated flow is reattached in the turbulent state for a short  
17 period after which a relaminarization process has occurred during the down-  
18 stroke motion (in which the level of hot-film signal is changed to its laminar  
19 value). A region with considerable wavelet magnitude at about the frequency  
20 range of 10-70 Hz. implies such a sharp variation with wide frequency content  
21 at around  $t/T = 0.5$ . More accurate, the higher portion of this range belongs  
22 to the transition events while the lower ones are concurrent with the LSB. It  
23 seems that very short region of turbulence causes the transition and relami-  
24 narization frequencies to be merged and appear as a peak region at this point.

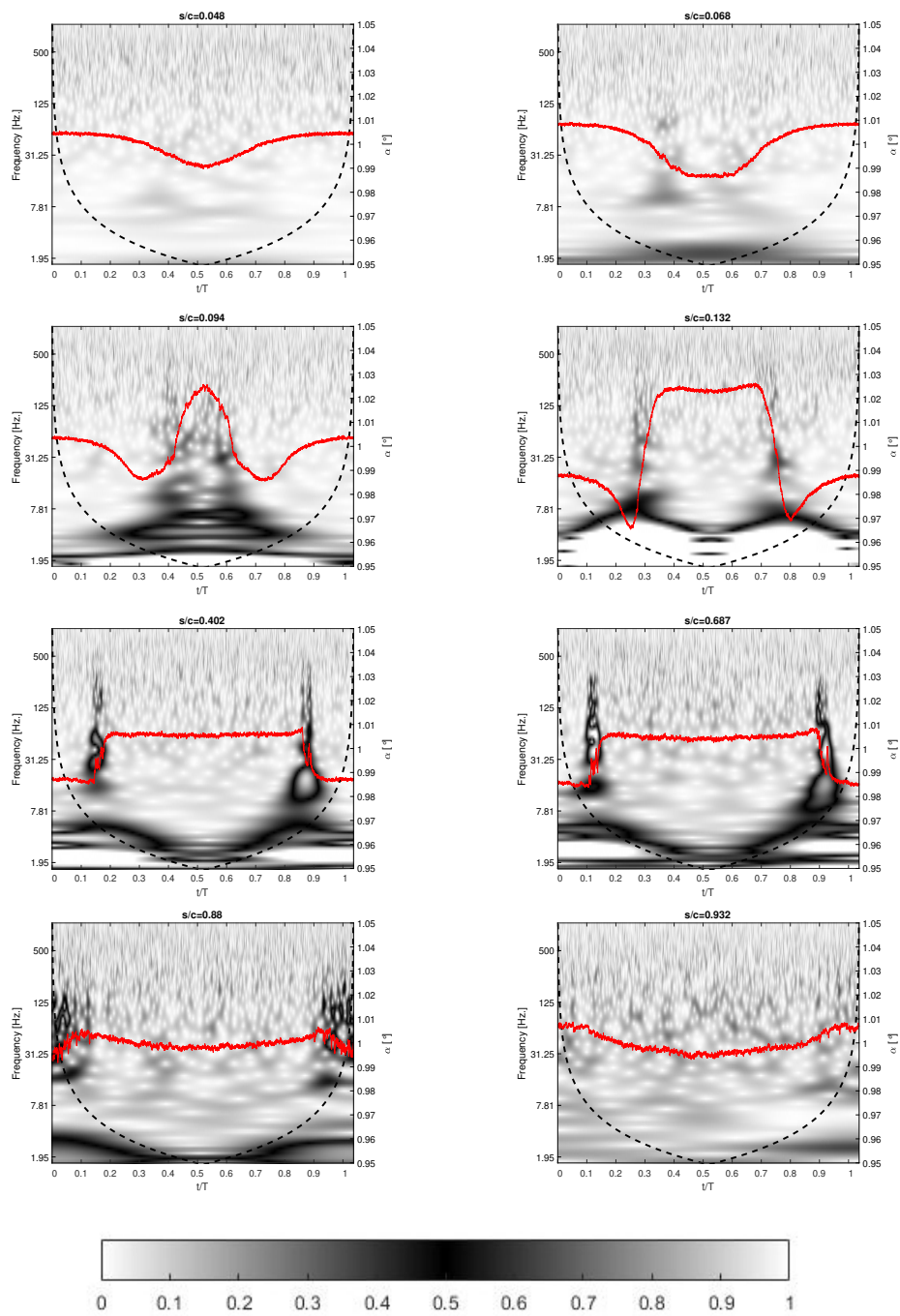


Figure 12: Contours of wavelet transform coefficients magnitudes along with hot-film signals at different positions over the upper surface

1 Farther down from the leading edge at  $s/c = 0.132$ , transition is captured with  
2 more turbulent state of the boundary layer during the motion in Fig. 12. It is  
3 worth nothing, compared with other cases that the amount of hot-film signal  
4 variations is the most significant, in both separation and reattachment states at  
5 this location. This implies existence of the LSB core which is pursued by the  
6 highest magnitude of shear stress. The development of the wavelet transform  
7 coefficient at this point shows a high frequency content within the laminar sep-  
8 aration bubble with diverse amplitudes. This behaviour is in agreement with  
9 the experimental [42] and DNS [43] visualisation results, and is due to vortex  
10 shedding within the laminar separation bubble zone. Jumping into  $s/c = 0.402$ ,  
11 one may perceive a more turbulent portion of the boundary layer state which  
12 has been expected due to being farther from the leading edge of the airfoil. The  
13 level of changes in hot-film signal in both laminar separation and reattachment  
14 moments are not as much as the previous point, which resembles this point  
15 to be far from the laminar separation bubble core. Rapid change of signal is  
16 also another important feature at this point exciting a great frequency interval  
17 of 25-210 Hz. Focusing on the raise part of the signal, it can be found that  
18 there is no separation zone after the laminar boundary layer since no signal  
19 decline can be observed when transitioning from the laminar to the turbulent  
20 state. As stated before, this indicates another transition mechanism which is  
21 different from the LSB. Here, the variety of dominant frequencies during differ-  
22 ent transition mechanisms is revealed. As demonstrated, the phenomena at LSB  
23 transition mechanism are relatively in lower range than those of the other mech-  
24 anism. The same features are observed at  $s/c = 0.687$ . However, the interval of  
25 fluctuation frequencies in the signal is increased to 12-280 Hz. representing the  
26 amplification of coherent structures such as the turbulent spots or flow streaks.  
27 For instance, a high amplitude fluctuation is observed at about  $t/T = 0.12$  and  
28 around the 50% intermittency point in the transition process which may con-  
29 tain dominant frequencies of approximately 37 and 61 Hz. More interestingly,  
30 the same phenomenon recurs with an identical frequency in the relaminariza-  
31 tion process. However, generally having focused on the two latter locations, an

1 asymmetry is clearly observed in frequency content of these locations expressing  
2 the difference between the transition and relaminarization processes.

3 Moving more towards the trailing edge, the characteristics of the hot-film  
4 signal at  $s/c = 0.88$ , it seems that regions with greater intensity of the wavelet  
5 transform belong to the small laminar zones of the signal at the initial and final  
6 instances of the motion. The flow is separated in the turbulent state at this  
7 point yielding in lower skin friction and signal level. Also at  $s/c = 0.932$  the  
8 flow seems to be fully separated roughly over the whole cycle and accordingly  
9 no particular phenomenon is felt on the surface.

10 At last, it should be noticed that below the dashed-line of Fig. 12, infor-  
11 mation in the scalogram should be treated as suspect due to the potential for  
12 edge effects. Above the dashed-line, the information provided by the scalo-  
13 gram is an accurate time-frequency representation of the data. This arises from  
14 non-existence of mathematically precise rule to determine the extent of the un-  
15 reliability at each scale [44, 45].

#### 16 4. Conclusion

17 A series of experimental tests were performed to figure out the behaviour  
18 of boundary layer transition over a pitching supercritical airfoil using hot-film  
19 sensors. The influences of reduced frequency and mean angle of attack were  
20 studied where, the start and the end of the transition and relaminarization were  
21 captured by the peak point in signal derivative and the 50% intermittency was  
22 obtained from the peak in standard deviation.

23 Two different transition mechanisms were recognized from the measure-  
24 ments. Laminar separation bubble was identified as the transition mechanism  
25 near the leading edge of the airfoil ( $s/c < 0.156$ ) and at higher AOAs ( $\alpha > 1^\circ$ ).  
26 Moving toward the trailing edge, the size and strength of the bubble were  
27 deemed to become shorter and weaker, so that at  $0.351c$  downstream of the  
28 leading edge, no bubble was found on the surface. At low AOAs, mostly less  
29 than  $1^\circ$ , however, the cause of boundary layer transition was differed from the

1 bubble. In essence, decrement of AOA is accompanying with the relaminar-  
2 ization process generated by presence of favorable pressure gradient. Also, on  
3 the last sensor near the trailing edge and at  $s/c = 0.932$ , signals of turbulent  
4 separation were seen at high AOAs. Increasing the reduced frequency eventu-  
5 ated in few results out of which are a delay in transition onset up to  $0.07t/T$  at  
6  $s/c = 0.932$  in case 2 and postponing it to a higher angle of attack, widening  
7 the hysteresis between the upstroke and downstroke motions and weakening or  
8 omission of vortical disturbances ensuing the removal of spikes in the signals.

9 The effects of mean AOA on movement of transition and relaminarization  
10 points were studied, indeed. For higher  $k$  the relaminarization point moves faster  
11 in higher mean AOA, while this process slowed down at negative AOAs. As  
12 expected, no important change was detected at lower  $k$  where the flow presumed  
13 to be quasi-steady.

14 An increase in the level of signal along with formation of higher frequency  
15 components (10 to 15 Hz.) while the state of flow is still laminar, implied de-  
16 velopment of the streamwise fluctuations and the concept of “laminar-kinetic-  
17 energy”. The frequency content within the laminar separation bubble confirmed  
18 the presence of vortex shedding and nonlinear modes interaction within the tran-  
19 sition region. The existence of another mechanism is also implied by the higher  
20 frequencies (up to 210 Hz.) emerge at the points farther from the leading edge.  
21 Furthermore, the wide range of frequencies in the transition and relaminariza-  
22 tion processes introduced the fact that multiple different coherent structures  
23 are produced in boundary layer. Finally, a time-frequency analysis showed  
24 that an asymmetry existed between the frequency content of the upstroke and  
25 downstroke motions, implying the difference between the transition and relam-  
26 inarization processes especially at locations farther down from the bubble zone  
27 toward the trailing edge.

1 **References**

- 2 [1] R. Mayle, The role of laminar-turbulent transition in gas turbine engines,  
3 International Gas Turbine and Aeroengine Congress and Exposition 77  
4 (1991) 500–520. doi:10.1017/S0022112004009851.
- 5 [2] J. Cornish, A Device for the Direct Measurements of Unsteady Air Flows  
6 and Some Characteristics of Boundary Layer Transition, Mississippi State  
7 University, Aerophysics Research Note 24 (1964).
- 8 [3] W. A. Cassels, J. F. Campbell, Boundary-layer transition study of sev-  
9 eral pointed bodies of revolution at supersonic speeds, Vol. 6063, National  
10 Aeronautics and Space Administration, 1970.
- 11 [4] F. Owen, Fluctuation and transition measurements in compressible bound-  
12 ary layers, in: 26th American Helicopter Society, Annual National Fo-  
13 rum, American Institute of Aeronautics and Astronautics, Reston, Virginia,  
14 1970. doi:10.2514/6.1970-745.
- 15 [5] R. A. Armistead, J. J. Keyes, A Study of Wall-Turbulence Phenomena  
16 Using Hot-Film Sensors, Journal of Heat Transfer 90 (1) (1968) 13. doi:  
17 10.1115/1.3597444.
- 18 [6] M. J. Moen, S. P. Schneider, The Effect of Sensor Size on the Performance  
19 of Flush-Mounted Hot-Film Sensors, Journal of Fluids Engineering 116 (2)  
20 (1994) 273. doi:10.1115/1.2910266.
- 21 [7] V. Schulte, H. P. Hodson, Unsteady Wake-Induced Boundary Layer Tran-  
22 sition in High Lift LP Turbines, Journal of Turbomachinery 120 (1) (1998)  
23 28. doi:10.1115/1.2841384.
- 24 [8] C. B. Lee, J. Z. Wu, Transition in Wall-Bounded Flows, Applied Mechanics  
25 Reviews 61 (3) (2008) 030802. doi:10.1115/1.2909605.
- 26 [9] K. H. HORSTMANN, A. QUAST, G. REDEKER, Flight and wind-tunnel  
27 investigations on boundary-layer transition, Journal of Aircraft 27 (2)  
28 (1990) 146–150. doi:10.2514/3.45910.

- 1 [10] E. GARTENBERG, W. G. JOHNSON, R. E. WRIGHT, D. L. CAR-  
2 RAWAY, C. B. JOHNSON, Boundary-layer transition-detection in a cryo-  
3 genic wind tunnel usinginfrared imaging, *AIAA Journal* 30 (2) (1992) 444–  
4 446. doi:10.2514/3.10936.
- 5 [11] M. Pascazio, J. Autric, D. Favier, C. Maresca, Unsteady boundary-layer  
6 measurement on oscillating airfoils - Transition and separation phenom-  
7 ena in pitching motion, in: 34th Aerospace Sciences Meeting and Ex-  
8 hibit, American Institute of Aeronautics and Astronautics, Reston, Vi-  
9 rginia, 1996. doi:10.2514/6.1996-35.
- 10 [12] D.-H. Kim, J.-W. Chang, Low-reynolds-number effect on the aerodynamic  
11 characteristics of a pitching naca0012 airfoil, *Aerospace Science and Tech-*  
12 *nology* 32 (1) (2014) 162 – 168. doi:https://doi.org/10.1016/j.ast.  
13 2013.08.018.
- 14 [13] A. Nati, R. de Kat, F. Scarano, B. W. van Oudheusden, Dynamic pitching  
15 effect on a laminar separation bubble, *Experiments in Fluids* 56 (9) (2015)  
16 172. doi:10.1007/s00348-015-2031-6.
- 17 [14] T. Leu, J. Yu, J. Miao, S. Chen, MEMS flexible thermal flow sensors  
18 for measurement of unsteady flow above a pitching wind turbine blade,  
19 *Experimental Thermal and Fluid Science* 77 (2016) 167–178. doi:10.1016/  
20 J.EXPTHERMFLUSCI.2016.04.018.
- 21 [15] Z. Vlahostergios, K. Yakinthos, A. Goulas, Separation-induced boundary  
22 layer transition: Modeling with a non-linear eddy-viscosity model coupled  
23 with the laminar kinetic energy equation, *International Journal of Heat*  
24 *and Fluid Flow* 30 (4) (2009) 617 – 636.
- 25 [16] K. Suluksna, P. Dechaumphai, E. Juntasaro, Correlations for modeling  
26 transitional boundary layers under influences of freestream turbulence and  
27 pressure gradient, *International Journal of Heat and Fluid Flow* 30 (1)  
28 (2009) 66 – 75.



- 1 [17] M. Bernardini, S. Pirozzoli, P. Orlandi, Compressibility effects on  
2 roughness-induced boundary layer transition, *International Journal of Heat  
3 and Fluid Flow* 35 (2012) 45 – 51, 7th Symposium on Turbulence & Shear  
4 Flow Phenomena (TSFP7).
- 5 [18] J. Serna, B. Lázaro, On the bursting condition for transitional separation  
6 bubbles, *Aerospace Science and Technology* 44 (2015) 43 – 50, instability  
7 and Control of Massively Separated Flows. doi:[https://doi.org/10.  
8 1016/j.ast.2014.10.010](https://doi.org/10.1016/j.ast.2014.10.010).
- 9 [19] G. L. O. Halila, A. P. Antunes, R. G. da Silva, J. L. F. Azevedo, Effects of  
10 boundary layer transition on the aerodynamic analysis of high-lift systems,  
11 *Aerospace Science and Technology* 90 (2019) 233 – 245. doi:[https://doi.  
12 org/10.1016/j.ast.2019.04.051](https://doi.org/10.1016/j.ast.2019.04.051).
- 13 [20] J. Xu, Z. Fu, J. Bai, Y. Zhang, Z. Duan, Y. Zhang, Study of boundary layer  
14 transition on supercritical natural laminar flow wing at high reynolds num-  
15 ber through wind tunnel experiment, *Aerospace Science and Technology* 80  
16 (2018) 221 – 231. doi:<https://doi.org/10.1016/j.ast.2018.07.007>.
- 17 [21] R. Vizinho, J. Morgado, J. Páscoa, M. Silvestre, Analysis of transitional  
18 flow in 3d geometries using a novel phenomenological model, *Aerospace  
19 Science and Technology* 45 (2015) 431 – 441. doi:[https://doi.org/10.  
20 1016/j.ast.2015.06.018](https://doi.org/10.1016/j.ast.2015.06.018).
- 21 [22] S. Kubacki, E. Dick, An algebraic model for bypass transition in turbo-  
22 machinery boundary layer flows, *International Journal of Heat and Fluid  
23 Flow* 58 (2016) 68 – 83.
- 24 [23] Q. Ye, F. F. Schrijer, F. Scarano, Geometry effect of isolated roughness on  
25 boundary layer transition investigated by tomographic piv, *International  
26 Journal of Heat and Fluid Flow* 61 (2016) 31 – 44, sI TSFP9 special issue.
- 27 [24] H. Medina, A. Beechook, H. Fadhila, S. Aleksandrova, S. Benjamin, A novel  
28 laminar kinetic energy model for the prediction of pretransitional velocity

- 1 fluctuations and boundary layer transition, *International Journal of Heat*  
2 *and Fluid Flow* 69 (2018) 150 – 163.
- 3 [25] J. Kiedaisch, M. Acharya, Investigation of unsteady separation over pitch-  
4 ing airfoils at high Reynolds numbers, in: 29th AIAA, Fluid Dynamics  
5 Conference, American Institute of Aeronautics and Astronautics, Reston,  
6 Virginia, 2013. doi:10.2514/6.1998-2975.
- 7 [26] S. J. Schreck, W. E. Faller, H. E. Helin, Pitch rate and reynolds number  
8 effects on unsteady boundary-layer transition and separation, *Journal of*  
9 *Aircraft* 35 (1) (1998) 46–52.
- 10 [27] T. Lee, S. Basu, Measurement of unsteady boundary layer developed on  
11 an oscillating airfoil using multiple hot-film sensors, *Experiments in Fluids*  
12 25 (2) (1998) 108–117. doi:10.1007/s003480050214.
- 13 [28] M. Tiedemann, F. Kost, Unsteady Boundary Layer Transition on a High  
14 Pressure Turbine Rotor Blade, in: Volume 3: Heat Transfer; Electric  
15 Power; Industrial and Cogeneration, ASME, 1999, p. V003T01A055. doi:  
16 10.1115/99-gt-194.
- 17 [29] T. Lee, P. Gerontakos, Investigation of flow over an oscillating air-  
18 foil, *Journal of Fluid Mechanics* 512 (2004) 313–341. doi:10.1017/  
19 S0022112004009851.
- 20 [30] S. Yarusevych, J. G. Kawall, P. E. Sullivan, Separated-shear-layer develop-  
21 ment on an airfoil at low reynolds numbers, *AIAA Journal* 46 (12) (2008)  
22 3060–3069. doi:10.2514/1.36620.
- 23 [31] M. Masdari, M. Jahanmiri, M. R. Soltani, A. Tabrizian, M. Gorji, Exper-  
24 imental investigation of a supercritical airfoil boundary layer in pitching  
25 motion, *Journal of Mechanical Science and Technology* 31 (1) (2017) 189–  
26 196. doi:10.1007/s12206-016-1221-3.
- 27 [32] A. Tabrizian, M. Masdari, F. Ehtehadi, Frequency analysis of a supercriti-  
28 cal airfoil boundary layer using discrete wavelet transform, in: 8th Interna-

- 1 tional Conference on Electrical, Computer, Mechanical and Mechatronics  
2 Engineering (ICE2018), Istanbul, Turkey, 2018.
- 3 [33] D. Rudmin, A. Benaissa, D. Poirel, Detection of Laminar Flow Separation  
4 and Transition on a NACA-0012 Airfoil Using Surface Hot-Films, *Journal*  
5 *of Fluids Engineering* 135 (10) (2013) 101104. doi:[10.1115/1.4024807](https://doi.org/10.1115/1.4024807).
- 6 [34] A. Poels, D. Rudmin, A. Benaissa, D. Poirel, Localization of Flow Sepa-  
7 ration and Transition Over a Pitching NACA0012 Airfoil at Transitional  
8 Reynolds Numbers Using Hot-Films, *Journal of Fluids Engineering* 137 (12)  
9 (2015) 124501. doi:[10.1115/1.4031008](https://doi.org/10.1115/1.4031008).
- 10 [35] M. Tatar, M. Tahani, M. Masdari, Numerical study of boundary layer  
11 transition using intermittency model, *Aircraft Engineering and Aerospace*  
12 *Technology* 91 (8) (2019) 1156–1168. doi:[10.1108/AEAT-05-2018-0144](https://doi.org/10.1108/AEAT-05-2018-0144).
- 13 [36] A. D. Gardner, K. Richter, Boundary layer transition determination for  
14 periodic and static flows using phase-averaged pressure data, *Experiments*  
15 *in Fluids* 56 (6) (2015) 119. doi:[10.1007/s00348-015-1992-9](https://doi.org/10.1007/s00348-015-1992-9).
- 16 [37] A. Goerttler, A. D. Gardner, K. Richter, Unsteady boundary layer tran-  
17 sition detection by automated analysis of hot film data, in: *Notes on Nu-*  
18 *merical Fluid Mechanics and Multidisciplinary Design*, Vol. 136, Springer,  
19 Cham, 2018, pp. 387–396. doi:[10.1007/978-3-319-64519-3\\_35](https://doi.org/10.1007/978-3-319-64519-3_35).
- 20 [38] A. Grossmann, J. Morlet, Decomposition of hardy functions into square in-  
21 tegrable wavelets of constant shape, *SIAM Journal on Mathematical Anal-*  
22 *ysis* 15 (4) (1984) 723–736. doi:[10.1137/0515056](https://doi.org/10.1137/0515056).
- 23 [39] M. Farge, Y. Guezennec, C. M. Ho, C. Meneveau, Continuous wavelet  
24 analysis of coherent structures, in: *Studying Turbulence Using Numerical*  
25 *Simulation Databases. 3: Proceedings of the 1990 Summer Program, 1990*,  
26 pp. 331–348.
- 27 [40] M. Farge, Wavelet transforms and their applications to turbulence, *Annual*  
28 *review of fluid mechanics* 24 (1) (1992) 395–458.

- 1 [41] The Path to Predicting Bypass Transition, Vol. Volume 1: Turbomachinery  
2 of Turbo Expo: Power for Land, Sea, and Air, v001T01A065. [doi:10.](https://doi.org/10.1115/96-GT-199)  
3 [1115/96-GT-199](https://doi.org/10.1115/96-GT-199).
- 4 [42] S. W. M. Lang, U. Rist, Investigations on disturbance amplification in a  
5 laminar separation bubble by means of lda and piv, 11th International  
6 Symposium on Laser Techniques to Fluid Mechanics, 2002, pp. 331–348.
- 7 [43] U. Rist, On instabilities and transition in laminar separation bubbles, in:  
8 Proc. CEAS Aerospace Aerodynamics Research Conference, 2002, pp. 10–  
9 12.
- 10 [44] H. Nobach, C. Tropea, L. Cordier, J.-P. Bonnet, J. Delville, J. Lewalle,  
11 M. Farge, K. Schneider, R. Adrian, Review of Some Fundamentals of Data  
12 Processing, Springer Berlin Heidelberg, Berlin, Heidelberg, 2007, pp. 1337–  
13 1398. [doi:10.1007/978-3-540-30299-5\\_22](https://doi.org/10.1007/978-3-540-30299-5_22).
- 14 [45] C. Torrence, G. P. Compo, A Practical Guide to Wavelet Analysis., Bulletin  
15 of the American Meteorological Society 79 (1) (1998) 61–78.